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A Distributed Merge and Split Algorithm for Fair Cooperation in Wireless Networks

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Abstract— This paper introduces a novel concept from coalitional game theory which allows the dynamic formation of coalitions among wireless nodes. A simple and distributed merge and split algorithm for coalition formation is constructed. This algorithm is applied to study the gains resulting from the cooperation among single antenna transmitters for virtual MIMO formation. The aim is to find an ultimate transmitters coalition structure that allows cooperating users to maximize their utilities while accounting for the cost of coalition formation. Through this novel game theoretical framework, the wireless network transmitters are able to self-organize and form a structured network composed of disjoint stable coalitions. Simulation results show that the proposed algorithm can improve the average individual user utility by 26.4% as well as cope with the mobility of the distributed users.

I. INTRODUCTION

Recently, cooperation between mobile devices has been one of the main activities of research work which tackled different aspects of cooperation at different layers. For instance, the problem of cooperation among single antenna receivers for virtual MIMO formation has been studied in [1] using coalitional game theory. The authors in [1] proved that for the receiver coalition game in a Gaussian interference channel and synchronous CDMA multiple access channel (MAC), a stable grand coalition of all users can form if *no cost* for cooperation is considered. Cooperation among single antenna transmitters and receivers in ad hoc networks has also been studied in [2]. The authors inspected the capacity gains that users can achieve while cooperating; namely at the transmitter side. Cooperation in wireless networks was also exploited at higher layers such as the network layer using game theory. For instance, cooperation in routing protocols was tackled in [3] where selfish nodes are allowed to cooperate for reducing the routing energy cost. In [4] and [5], the nodes along the route can cooperate with each other in order to improve the link quality or reduce the power consumption. Cooperation for packet forwarding is studied in [6] and [7] using cooperative game theory, repeated game theory, and machine learning. Auction theory is used in [8] for optimizing relay resource allocation in cooperative networks. Thus, previous work mainly focused on the study of the gains resulting from virtual MIMO as well as from

higher layer cooperation. For virtual MIMO, the usage of coalitional games was limited to the study of the formation of the grand coalition when the users cooperate without cost. However, due to cooperation costs, it might not be beneficial for users located far away from each other to cooperate.

The main contribution of this article is to derive a fair cooperation strategy among distributed single antenna transmitters, which will allow these users to self-organize into structured coalitions while maximizing their utilities with cost. For this purpose, we construct a coalition formation algorithm based on a novel concept from coalitional game theory which, to our knowledge, have not been used in the wireless world yet. A simple and distributed merge and split algorithm is devised for forming the coalitions. Through this algorithm, we seek to find the possible coalition structures in the transmitter cooperation game. The convergence of the algorithm is proven and the stability of the resulting partitions is investigated. Different fairness criteria for dividing the extra benefits among the coalition users are also discussed.

The rest of this paper is organized as follows: Section II presents the system model. In Section III, we present the proposed algorithm, prove its properties and discuss the fairness criteria. Simulation results are presented and analyzed in Section IV. Finally, conclusions are drawn in Section V.

II. SYSTEM MODEL

Consider a network having M_t single antenna transmitters, e.g. mobile users, sending data in the uplink to a fixed receiver, e.g. a base station, with M_r receivers (Multiple Access Channel). Denote $N = \{1 \dots M_t\}$ as the set of all M_t users in the network, and let $S \subset N$ be a coalition consisting of $|S|$ users. We consider a TDMA transmission in the network, thus, in a non-cooperative manner, the M_t users require a time scale of M_t slots since every user occupies one slot. When cooperating, the single antenna transmitters form different disjoint coalitions and the coalitions will subsequently transmit in a TDMA manner, that is one coalition per transmission. Thus, during the time scale M_t , each coalition is able to transmit within all the time slots previously held by its users. In addition, similar to [2] we define a fixed transmitting power constraint \bar{P} per time slot (i.e. per coalition) which is the power available for all transmitters that will occupy this slot. If a coalition (viewed as a single user MIMO after cooperation) will occupy the slot, part of the transmit power constraint will be used for

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actual transmission while the other part will constitute a cost for the exchange of information between the members of the coalition. This cost is taken as the sum of the powers required by *each* user in a coalition S to broadcast to its corresponding farthest user inside S . For instance, the power needed for broadcast transmission between a user $i \in S$ and its corresponding farthest user $\hat{i} \in S$ is given by

$$\bar{P}_{i,\hat{i}} = \frac{\nu_0 \cdot \sigma^2}{h_{i,\hat{i}}^2}, \quad (1)$$

where ν_0 is a target SNR for information exchange, σ^2 is the noise variance and $h_{i,\hat{i}} = \sqrt{\kappa/d_{i,\hat{i}}^\alpha}$ is the path loss between users i and \hat{i} ; κ being the path loss constant, α the path loss exponent and $d_{i,\hat{i}}$ the distance between users i and \hat{i} . In consequence, the total power cost for a coalition S having $|S|$ users is given by \hat{P}_S as follows

$$\hat{P}_S = \sum_{i=1}^{|S|} \bar{P}_{i,\hat{i}}. \quad (2)$$

It is interesting to note that the defined cost depends on the location of the users and the size of the coalition; hence a higher power cost is incurred whenever the distance between the users increases or the coalition size increases. Thus, the actual power constraint per coalition S is given by

$$P_S = (\tilde{P} - \hat{P}_S)^+, \text{ with } a^+ \triangleq \max(a, 0) \quad (3)$$

In the considered TDMA system, each coalition transmits in a time slot, hence, perceiving no interference from other coalitions during transmission. Therefore, in a time slot, the sum-rate of the virtual MIMO system formed by a coalition S , assuming Gaussian signalling and under a power constraint P_S , is given by [9] as

$$C_S = \max_{\mathbf{Q}_S} I(\mathbf{x}_S; \mathbf{y}_S) = \max_{\mathbf{Q}_S} \log \det(\mathbf{I}_{M_r} + \mathbf{H}_S \cdot \mathbf{Q}_S \cdot \mathbf{H}_S^\dagger), \quad (4)$$

where \mathbf{x}_S and \mathbf{y}_S are, respectively, the transmitted and received signal vectors of coalition S , $\mathbf{Q}_S = \mathbb{E}[\mathbf{x}_S \cdot \mathbf{x}_S^\dagger]$ is the covariance of \mathbf{x}_S with $\text{tr}[\mathbf{Q}_S] \leq P_S$ and \mathbf{H}_S is the $M_r \times M_t$ channel matrix with \mathbf{H}_S^\dagger its conjugate transpose.

In this work, we consider a path-loss based deterministic channel matrix \mathbf{H}_S assumed perfectly known at the transmitter and receiver with each element $h_{i,j} = \sqrt{\kappa/d_{i,j}^\alpha}$ with $d_{i,j}$ the distance between transmitter i and receiver j . For such a channel, the work in [9] shows that the maximizing input signal covariance \mathbf{Q}_S is given by $\mathbf{Q}_S = \mathbf{V}_S \mathbf{D}_S \mathbf{V}_S^\dagger$; with $\text{tr}[\mathbf{D}_S] = \text{tr}[\mathbf{Q}_S]$ where \mathbf{V}_S is the unitary matrix given by the singular value decomposition of $\mathbf{H}_S = \mathbf{U}_S \mathbf{\Sigma}_S \mathbf{V}_S^\dagger$. \mathbf{D}_S is an $M_t \times M_t$ diagonal matrix given by $\mathbf{D}_S = \text{diag}(D_1, \dots, D_K, 0, \dots, 0)$ where $K \leq \min(M_r, M_t)$ represents the number of positive singular values of \mathbf{H}_S (eigenmodes) and each D_i given by

$$D_i = (\mu - \lambda_i^{-1})^+. \quad (5)$$

μ is determined by water-filling to satisfy the coalition power constraint $\text{tr}[\mathbf{Q}_S] = \text{tr}[\mathbf{D}_S] = \sum_i D_i = P_S$ and

λ_i represents the i th eigenvalue of $\mathbf{H}_S^\dagger \mathbf{H}_S$. Hence, based on [9], the resulting capacity for a coalition S is given by $C_S = \sum_{i=1}^K (\log(\mu \lambda_i))^+$.

Consequently, over the TDMA time scale of M_t , for every coalition $S \subset N$, we define the utility function as

$$v(S) = \begin{cases} |S| \cdot C_S, & \text{if } P_S > 0, \\ 0, & \text{otherwise.} \end{cases} \quad (6)$$

This utility represents the total capacity achieved by coalition S during the time scale M_t while accounting for the cost through the power constraint. The second case states that if the power cost within a coalition is larger than or equal the constraint, then the coalition cannot form. Thus, we have a coalitional game (N, v) with a transferable utility and we seek, through coalition formation, a coalition structure that will allow the users to maximize their utilities in terms of rate with cost in terms of power.

III. COALITION FORMATION

A. Coalition Formation Algorithm

Unlike existing literature, in the proposed transmitter cooperation (N, v) game, we will prove that the grand coalition cannot form due to cost.

Definition 1: A coalitional game (N, v) with a transferable utility is said to be superadditive if for any two disjoint coalitions $S_1, S_2 \subset N$, $v(S_1 \cup S_2) \geq v(S_1) + v(S_2)$.

Theorem 1: The proposed transmitter (N, v) coalitional game with cost is, in general, non-superadditive.

Proof: Consider two disjoint coalitions $S_1 \subset N$ and $S_2 \subset N$ in the network, with the users of $S_1 \cup S_2$ located far enough to yield a power cost per (2) $\hat{P}_{S_1 \cup S_2} > \tilde{P}$. Therefore, by (3) $P_{S_1 \cup S_2} = 0$ yielding $v(S_1 \cup S_2) = 0 < v(S_1) + v(S_2)$ (6); hence the game is not superadditive. ■

Definition 2: A payoff vector $\mathbf{z} = (z_1, \dots, z_{M_t})$ is said to be *group rational* or *efficient* if $\sum_{i=1}^{M_t} z_i = v(N)$. A payoff vector \mathbf{z} is said to be *individually rational* if the player can obtain the benefit no less than acting alone, i.e. $z_i \geq v(\{i\}) \forall i$. An *imputation* is a payoff vector satisfying the above two conditions.

Definition 3: An imputation \mathbf{z} is said to be unstable through a coalition S if $v(S) > \sum_{i \in S} z_i$, i.e., the players have incentive to form coalition S and reject the proposed \mathbf{z} . The set \mathcal{C} of stable imputations is called the *core*, i.e.,

$$\mathcal{C} = \left\{ \mathbf{z} : \sum_{i \in N} z_i = v(N) \text{ and } \sum_{i \in S} z_i \geq v(S) \forall S \subset N \right\}. \quad (7)$$

A non-empty core means that the players have an incentive to form the grand coalition.

Theorem 2: In general, the core of the proposed (N, v) coalitional game is empty.

Proof: Similarly to the proof of Theorem 1, consider a TDMA network composed of only two disjoint coalitions S_1 and S_2 with $v(S_1 \cup S_2 = N) = 0$. In this case, no imputation can be found to lie in the core, since the value of the grand

TABLE I
ONE STAGE OF THE PROPOSED MERGE AND SPLIT ALGORITHM

Step 1: Coalition Formation Phase: Arbitrary Merge and Split Rules
Step 2: Transmission Phase: One Coalition per Slot

coalition is $v(N) = 0$. Thus, in such a case, S_1 and S_2 will have a better performance in a non-cooperative mode and the core of the transmitter cooperation (N, v) game is empty. ■

As a result of the non-superadditivity of the game and the emptiness of the core, the grand coalition does *not* form among cooperating transmitters. Instead, independent disjoint coalitions will form in the network. Therefore, we seek a novel algorithm for coalition formation that accounts for the properties of the transmitter cooperation game with cost.

An interesting approach for coalition formation through simple merge and split operations is given by [10]. We define a *collection* of coalitions S in the grand coalition N as the family $S = \{S_1, \dots, S_l\}$ of mutually disjoint coalitions S_i of N . In other words, a collection is any arbitrary group of disjoint coalitions S_i of N not necessarily spanning all players of N . In addition, a collection S of coalitions encompassing all the players of N , that is $\bigcup_{j=1}^l S_j = N$ is called a *partition* of N . Moreover, the merge and split rules defined in [10] are simple operations that allow to modify a partition T of N as follows

- **Merge Rule:** Merge any set of coalitions $\{S_1, \dots, S_k\}$ where $\sum_{j=1}^k v(S_j) < v(\bigcup_{j=1}^k S_j)$; thus $\{S_1, \dots, S_k\} \rightarrow \bigcup_{j=1}^k S_j$.
- **Split Rule:** Split any set of coalitions $\bigcup_{j=1}^k S_j$ where $\sum_{j=1}^k v(S_j) > v(\bigcup_{j=1}^k S_j)$; thus $\bigcup_{j=1}^k S_j \rightarrow \{S_1, \dots, S_k\}$.

As a result, a group of coalitions (or users) decides to merge if it is able to improve its total utility through the merge; while a coalition splits into smaller coalitions if it is able to improve the total utility. Moreover, it is proven in [10] that any iteration of successive arbitrary merge and split operations *terminates*.

A coalition formation algorithm based on merge and split can be formulated for wireless networks. For instance, for the transmitter cooperation game, each stage of our coalition formation algorithm will run in two consecutive phases shown in Table I: adaptive coalition formation, and then transmission. During the coalition formation phase, the users form coalitions through an iteration of arbitrary merge and split rules repeated until termination. Following the self organization of the network into coalitions, TDMA transmission takes place with each coalition transmitting in its allotted slots. Subsequently, the transmission phase may occur several times prior to the repetition of the coalition formation phase, notably in low mobility environments where changes in the coalition structure due to mobility are seldom.

B. Stability Notions

The work done in [10] studies the stability of a partition through the concept of defection function.

Definition 4: A *defection* function \mathbb{D} is a function which associates with any arbitrary partition $T = \{T_1, \dots, T_l\}$ (each T_i is a coalition) of the players set N a family (i.e. group) of collections in N .

Two important defection functions can be pinpointed. First, the $\mathbb{D}_{hp}(T)$ function (\mathbb{D}_{hp}) which associates with each partition T of N the family of all partitions of N that the players can form through merge and split operations applied to T . This function allows any group of players to leave the partition T of N through *merge and split* operations to create another *partition* in N . Second, the $\mathbb{D}_c(T)$ function (\mathbb{D}_c) which associates with each partition T of N the family of all collections in N . This function allows any group of players to leave the partition T of N through *any* operation and create an arbitrary *collection* in N . Two forms of stability stem from these definitions: \mathbb{D}_{hp} stability and a stronger strict \mathbb{D}_c stability. In fact, a partition T is \mathbb{D}_{hp} -stable, if no players in T are interested in leaving T through merge and split to form other partitions in N ; while a partition T is strictly \mathbb{D}_c -stable, if no players in T are interested in leaving T to form other collections in N (not necessarily by merge and split).

Theorem 3: Every partition resulting from our proposed merge and split algorithm is \mathbb{D}_{hp} -stable.

Proof: A network partition T resulting from the proposed merge and split algorithm can no longer be subject to any additional merge or split operations as successive iteration of these operations terminate [10]. Therefore, the users in the final network partition T cannot leave this partition through merge and split and the partition T is immediately \mathbb{D}_{hp} -stable. ■

Nevertheless, a stronger form of stability can be sought using strict \mathbb{D}_c -stability. The appeal of a strictly \mathbb{D}_c stable partition is two fold [10]: 1) it is the unique outcome of any arbitrary iteration of merge and split operations done on any partition of N ; 2) it is a partition that maximizes the social welfare which is the sum of the utilities of all coalitions in a partition. However, the existence of such a partition is not guaranteed. In fact, the authors in [10] showed that a partition $T = \{T_1, \dots, T_l\}$ of the whole space N is strictly \mathbb{D}_c -stable only if it can fulfill two necessary and sufficient conditions:

- 1) For each $i \in \{1, \dots, l\}$ and each pair of disjoint *coalitions* S_1 and S_2 such that $\{S_1 \cup S_2\} \subset T_i$ we have $v(S_1 \cup S_2) > v(S_1) + v(S_2)$.
- 2) For the partition $T = \{T_1, \dots, T_l\}$ a coalition $G \subset N$ formed of players belonging to different $T_i \in T$ is T -incompatible, that is for no $i \in \{1, \dots, l\}$ we have $G \subset T_i$. Strict \mathbb{D}_c -stability requires that for all T -incompatible coalitions G , $\sum_{i=1}^l v(T_i \cap G) > v(G)$.

Therefore, in the case where a partition T of N satisfying the above two conditions exists; the proposed algorithm converges to this optimal strictly \mathbb{D}_c -stable partition since it constitutes a unique outcome of any arbitrary iteration of merge and split. However, if no such partition exists, the proposed algorithm yields a final network partition that is \mathbb{D}_{hp} -stable. In the transmitter cooperation game, the first condition of \mathbb{D}_c -stability depends on the users location in the network

due to cost of cooperation. In fact, it is well known [9] that, in an ideal case with no cost for cooperation, as the number of transmit antennas are increased for a fixed power constraint, the overall system's diversity increases. In fact, consider a partition $T = \{T_1, \dots, T_l\}$ of N , and any two disjoint coalitions S_1 and S_2 such that $\{S_1 \cup S_2\} \subset T_i$. Assuming that no cost for cooperation exists, the capacity of the coalition $S_1 \cup S_2$, denoted $C_{S_1 \cup S_2}$, is larger than the capacities C_{S_1} and C_{S_2} of the coalitions S_1 and S_2 acting non-cooperatively (due to the larger number of antennas in $S_1 \cup S_2$); thus $|S_1 \cup S_2| \cdot C_{S_1 \cup S_2} > |S_1 \cup S_2| \cdot \max(C_{S_1}, C_{S_2})$ with $|S_1 \cup S_2| = |S_1| + |S_2|$. As a result $C_{S_1 \cup S_2}$ satisfies

$$|S_1 \cup S_2| \cdot C_{S_1 \cup S_2} > |S_1| \cdot C_{S_1} + |S_2| \cdot C_{S_2}. \quad (8)$$

In fact, (8) yields $v(S_1 \cup S_2) > v(S_1) + v(S_2)$ which is the necessary condition to verify the first \mathbb{D}_c -stability condition. However, due to the cost given by (2) $C_{S_1 \cup S_2}$, C_{S_1} and C_{S_2} can have different power constraints due to the power cost, i.e. users location, and this condition is not always verified. Therefore, in practical networks, guaranteeing the first condition for existence of a strictly \mathbb{D}_c -stable partition is random due to the random location of the users. Furthermore, for a partition $T = \{T_1, \dots, T_l\}$, the second condition of \mathbb{D}_c -stability is also dependent on the distance between the users in different coalitions $T_i \in T$. In fact, as previously defined, for a partition T a T-incompatible coalition G is a coalition formed out of users belonging to different $T_i \in T$. In order to always guarantee that $\sum_{i=1}^l v(T_i \cap G) > v(G)$ it suffice to have $v(G) = 0$ for all T-incompatible coalitions G . In a network partition T where the players belonging to different coalitions $T_i \in T$ are separated by large distances, any T-incompatible coalition G will have $v(G) = 0$ based on (6) and, thus, satisfying the second \mathbb{D}_c -stability condition.

Finally, the proposed algorithm can be implemented in a distributed way. Since the user can detect the strength of the other users' uplink signals, the nearby users can be discovered. By using a signalling channel, the distributed users can exchange some channel information and then perform the merge and split algorithm. The signalling for this handshaking can be minimal.

C. Fairness Criteria for Distributions within Coalition

In this section, we present possible fairness criteria for dividing the coalition worth among its members.

1) *Equal Share Fairness*: The most simple division method is to divide the *extra* equally among users. In other words, the utility of user i among the coalition S is

$$z_i = \frac{1}{|S|} \left(v(S) - \sum_{j \in S} v(\{j\}) \right) + v(\{i\}). \quad (9)$$

2) *Proportional Fairness*: The equal share fairness is a very simple and strict fairness criterion. However, in practice, the user experiencing a good channel might not be willing to cooperate with a user under bad channel conditions, if the extra is divided equally. To account for the channel differences,

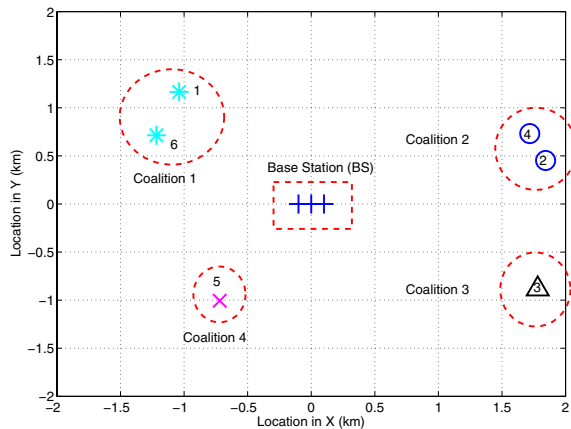


Fig. 1. A snapshot example of coalition formation.

we use another fairness criterion named proportional fairness, in which the extra benefit is divided in weights according to the users' non-cooperative utilities. In other words,

$$z_i = w_i \left(v(S) - \sum_{j \in S} v(\{j\}) \right) + v(\{i\}), \quad (10)$$

where $\sum_{i \in S} w_i = 1$ and within the coalition

$$\frac{w_i}{w_j} = \frac{v(\{i\})}{v(\{j\})}, \quad (11)$$

IV. SIMULATION RESULTS

For simulations, the base station (BS) is placed at the origin with $M_r = 3$ antennas, and random users are located within a square of $2 \text{ km} \times 2 \text{ km}$ around the BS. The power constraint per slot is $\hat{P} = 0.01 \text{ W}$, the SNR for information exchange is $\nu_0 = 10 \text{ dB}$ and the noise level is -90 dBm . The propagation loss is $\alpha = 3$ and $\kappa = 1$.

In Fig. 1, we show a snapshot of a network with $M_t = 6$ users. Using the proposed merge and split protocol, clusters of users are formed for distributed closely located users. Moreover, the coalition structure in Fig. 1 is strictly \mathbb{D}_c -stable, thus, it is the unique outcome of any iteration of merge and split. The strict \mathbb{D}_c stability of this structure is immediate since a partition verifying the two conditions of Section III-B exists. For the first condition, strict superadditivity within the coalitions is immediately verified by merge rule due to having two users per formed coalition. For the second condition, any T-incompatible coalition will have a utility of 0 since the users in the different formed coalitions are too far to cooperate. For example, consider the T-incompatible coalition $\{2, 3\}$, the distance between users 3 and 2 is 1.33 km yielding per (1) and (2) a power cost $\hat{P}_{\{2,3\}} = 0.052 \text{ W} > \hat{P} = 0.01 \text{ W}$ thus, by (6) $v(\{2, 3\}) = 0$. This result is easily verifiable for all T-incompatible coalitions.

In Fig. 2, we show how the algorithm handles mobility. The network setup of Fig. 1 is used and User 6 moving from the left to right for 2.8 km . When User 6 moves to the right

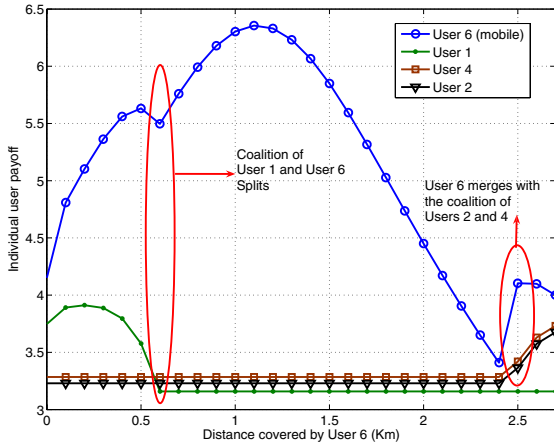


Fig. 2. Coalition merging/splitting due to mobility.

TABLE II

PAYOFF DIVISION ACCORDING TO DIFFERENT FAIRNESS

	User 2	User 4	User 6
Equal division	3.7310	3.6761	3.9993
Proportional fair	3.6155	3.6968	4.0940

first, it becomes closer to the BS and its utility increases and so does the utility of User 1. However, when the distance between Users 1 and 6 increases, the cost increases and both users' payoffs drop. As long as the distance covered by User 6 is less than 0.6 Km, the coalition of Users 1 and 6 can still bring mutual benefits to both users. After that, splitting occurs and User 1 and User 6 transmit independently. When User 6 move about 1.2 Km, it begins to distance itself from the BS and its utility begins to decrease. When User 6 moves about 2.5 km, it will be beneficial to users 2, 4 and 6 to form a 3-user coalition through the merge rule since $v(\{2, 4, 6\}) = 10.8883 > v(\{2, 4\}) + v(\{6\}) = 6.5145 + 3.1811 = 9.6956$. As User 6 moves further away from the BS, User 2 and User 4's utilities are improved within coalition $\{2, 4, 6\}$, while User 6's utility decreases slower than prior to merge.

Table II shows the payoff division among coalition users when the mobile User 6 moves 2.7 km in Fig. 2. In this case, we have $v(\{2\}) = 2.4422$, $v(\{4\}) = 2.4971$, $v(\{6\}) = 2.7654$ and $v(\{2, 4, 6\}) = 11.4063$. Compared with the equal division, proportional fairness gives User 6 the highest share of the extra benefit and User 2 the lowest share because User 6 has a higher non-cooperative utility than User 2. Thus, Table II shows how different fairness criteria can yield different apportioning of the extra cooperation benefits.

In Fig. 3, we show the average individual user payoff improvement as a function of the number of users in the networks. Here we run the simulation for 10000 different random locations. For cooperation with coalitions, the average individual utility increases with the number of users while for the non-cooperative approach an almost constant performance is noted. Cooperation presents a clear performance advantage reaching up to 26.4% improvement of the average user payoff at $M_t = 50$ as shown in Fig. 3.

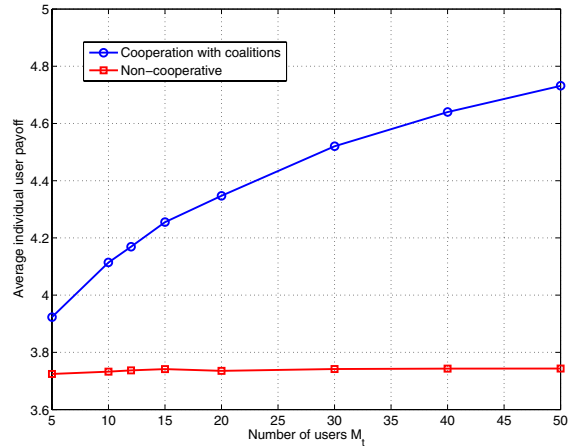


Fig. 3. Performance improvement.

V. CONCLUSIONS

In this paper, we construct a novel game theoretical algorithm suitable for modeling distributed cooperation with cost among single antenna users. Unlike existing literature which sought algorithms to form the grand coalition of transmitters; we inspected the possibility of forming disjoint independent coalitions which can be characterized by novel stability notions from coalitional game theory. We proposed a simple and distributed merge and split algorithm for forming coalitions and benefiting from spatial gains. Various properties of the algorithm are exposed and proved. Simulation results show how the derived algorithm allows the network to self-organize while improving the average user payoff by 26.4% and efficiently handling the distributed users' mobility.

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