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▶ **To cite this version:**

Enrico Zio, L. R. Golea, Giovanni Sansavini. Optimizing protections against cascades in network systems: A modified binary differential evolution algorithm. Reliability Engineering and System Safety, 2012, 103, pp.72-83. 10.1016/j.ress.2012.03.007 . hal-00777140

HAL Id: hal-00777140

https://centralesupelec.hal.science/hal-00777140

Submitted on 16 Jan 2013

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Optimizing protections against cascades in network systems: a modified binary differential evolution algorithm

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Abstract – This paper addresses the optimization of protection strategies in critical infrastructures within a complex network systems perspective. The focus is on cascading failures triggered by the intentional removal of a single network component. Three different protection strategies are proposed that minimize the consequences of cascading failures on the entire system, on predetermined areas or on both scales of protective intervention in a multi-objective optimization framework. We optimize the three protection strategies by devising a modified binary differential evolution scheme that overcomes the combinatorial complexity of this optimization problem. We exemplify our methodology with reference to the topology of an electricity infrastructure, i.e. the 380 kV Italian power transmission network. We only focus on the structure of this network as a test case for the suggested protection strategies, with no further reference on its physical and electrical properties.

Keywords: critical infrastructure; network protection; line switching; cascading failure; differential evolution algorithm; multi-objective optimization.

1 Introduction

Engineered critical infrastructures (CIs) are the systems of interest in this work as of fundamental importance for the sustainment of modern Societies. The motivation is that they provide the continuous flow of essential goods (e.g. energy, water, data) and services (e.g. banking, health care, transportation) which the welfare and security of our nations rely on. Their security against cascading failures, triggered by random failures or malevolent acts, is a priority for all developed Countries.

Network interdiction (NI) is a common approach for the identification of opportunities for choosing components, allocating redundancies or modifying the system with the aim of strengthening ('hardening') a CI. The approach consists in finding a set of network elements, usually links, to be interdicted in order to minimize the maximum flow that can be transmitted between any two (or among any) specific nodes. The underlying idea is that the identification of those components or groups of components whose damage yields the largest disruption to the network, provides indications on how to protect for improving its safety and security. Several models have been developed for identifying optimal NI strategies, i.e. sets of attacks/failures that cause the largest possible disruption given minimum or limited offensive resources [Dai and Poh, 2002; Arroyo and Fernandez, 2009; Rocco and Ramirez, 2009].

For large networks, the combinatorial problems which arise from the search among the multiple interdiction scenarios, have been tackled by heuristic algorithms like Genetic Algorithms (GAs) [Arroyo and Fernandez, 2009], metaheuristic algorithms like greedy algorithms [Bier et al., 2007] or non-linear programming [Salmeron et al., 2004]. However, these methods fail to represent the aftermath of an attack or failure, i.e. to account for the propagation of the initial disturbance in the network by cascading failures. Furthermore, hardening the network by modifications, i.e. via replacement of components or addition of redundancies, can be difficult, slow and expensive.

A more feasible alternative is network protection (NP) by line switching, done automatically or by a system operator, following an attack or a failure. In the energy field, this is common practice in problems like line overloads [Granelli et al., 2006], loss and/or cost reductions [Schnyder and Glavitsch, 1990], system security improvements [Schnyder and Glavitsch, 1988], or a combination of them [Shao and Vittal, 2005]. Other examples of line switching are the traffic closure due to road work, accidents or natural disasters, interruption of internet or telecommunication lines. Unlike NI, that aims at hindering failure propagation in a passive way, i.e. by designing components and allocating redundancies to avoid failures, NP aims at hindering failure propagation by cutting off the possible "directions" along which failures can spread within the network. The strategy for such protection stands on the possibility of finding the optimal set of lines to be cut-off in order to limit the consequences of cascade failures; in large networks, this poses a combinatorial optimization problem.

In this paper, we offer a complex network perspective on the NP problem. This approach aims at characterizing the topology of network systems and identifying critical parts by an analysis that is preliminary and complementary to more detailed and realistic approaches [Bier et al., 2007; Dobson et al., 2007; Hines et al., 2010; Salmeron et al., 2004]. The feasibility of line switching is evaluated by a model of cascading failure process which relies on a topological representation of the network connection pattern [Zio and Sansavini, 2009]. The abstract model of flow and cascades is not based on the physics of the actual power flow but rather mimics the flow in the network based on the shortest paths that connect generation and load nodes. The topological, abstract representation is useful for preliminary vulnerability analysis of CIs; it requires minimum information on the network but is capable of identifying critical elements with respect to the structure, i.e. edges and nodes whose failure can induce a severe structural damage to the network and split it into isolated clusters [Eusgeld et al., 2009]. This modeling entails considering the interplay between structural characteristics and dynamical aspects and provides indications on the elements critical for the failure propagation process [Zio and Sansavini, 2010], and on the actions that prevent or mitigate undesired effects [Motter, 2004]. Moreover, these models shed light on the way complex networks react to faults and attacks, evaluating their consequences when propagation dynamics are taken into account. The system response often results in a dramatic cascade phenomenon due to avalanches of node outages.

Abstract modeling paradigms [Dobson et al., 2005; Hines and Blumsack, 2008; Holme, 2002; Kinney et al., 2005; Motter and Lai, 2002] are introduced in the analysis of CIs to fulfill two main objectives: (I) helping to identify preliminary vulnerabilities of critical infrastructures by topology-driven and dynamical analysis, (II) to guide and focus further detailed analyses of critical areas of the CIs. However, given the somewhat abstract level of the modeling supporting topological analysis, the results gained with respect to the vulnerable points (or lines) in the system (first findings) may not be clear-cut, and major hidden vulnerabilities may still be expected. Then, to achieve a higher degree of accuracy, system understanding has to be further developed and more detailed information about the system and its operating environment may be needed. The re-assessment of simplifications made earlier may call for more sophisticated methods of their successive in-depth analysis [Kroger and Zio, 2011]. In order to draw firm conclusions about the significance of topological methods, e.g. in electricity infrastructure vulnerability, current research

focuses on systematically comparing the results from power-flow based vulnerability models with those from graph theoretic models of vulnerability [Hines et al., 2010; Rosato et al., 2009; Zio et al., 2011]. The general impression is that there is only a partial superposition of functional and structural criticalities. In this respect, the abstract model of flow and cascading that is used in this study, is not validated as an approximation to real or simulated data.

The combinatorial optimization problem of identifying the optimal set of lines to be cut-off in order to limit the consequences of cascade failures is addressed by a modified version of the binary differential evolution (MBDE) algorithm [Wang et al., 2010]. Differential Evolution (DE) is an emerging population-based stochastic optimization technique [Storn and Price, 1995]. The standard DE algorithm is simple and efficient and has been successfully applied in various scientific and engineering fields [Greem and Kim, 2001; Mahdavi et al., 2007; Coelho and Bernert, 2008; Saka, 2009], often with superior performance than alternative optimization algorithms, e.g. particle swarm optimization and GAs [Ponsich and Coello, 2009]. MBDE is a novel binary version of DE developed to tackle binary-coded optimization problems [Wang et al., 2010]: thus, it is suitable to solve our discrete combinational NP optimization problem.

The rest of the paper is organized as follows: Section 2 describes the basis of the adopted model of cascading failures. Section 3 presents the suggested NP strategies. The description of the MBDE algorithm is provided in Section 4 and its application to NP optimization in a case study, i.e. the topological structure of the Italian 380kV power transmission grid, is conducted in Section 5. Section 6 provides conclusions and points out directions for future work.

2. The model of cascading failures in network systems

We adopt an abstract modeling framework, which allows analyzing in an effective way the extent to which the failure propagation process affects the network system and to devise prevention or mitigation of the undesired effects [Motter and Lai, 2002, Dobson et al., 2005]. The abstraction is founded on a topological representation of a network of N nodes (these would be the buses in an electric power grid) and K edges (these would be the electrical lines). The topological representation abstracts the physical properties of the elements of the network to highlight its structural properties. Two types of nodes are distinguished here: N_G source nodes and N_D sink nodes. In order to abstractly account for the flow of the physical quantities in the network, we assume that it is transmitted along the source-sink shortest paths [Batagelj, 1994; Motter and Lai, 2002; Albert et al., 2004; Newman and Girvan, 2004; Latora and Marchiori, 2005; Duenas-Osorio and Vemuru, 2009; Zio and Sansavini, 2010].

We model the load on a component, e.g. a node or line, as dependent on the number of shortest paths transiting through it, when flow is sent from each available source node to each sink node. In this view, the load, L_j, or amount of flow passing through a node, is measured by the node betweenness [Sabidussi, 1966; Nieminen, 1974; Freeman, 1978; Freeman, et al. 1991; Little, 2002]:

$$L_j = \frac{1}{(N-1)(N-2)} \sum_{i \in N_G, j \in N_D, i \neq j \neq k} \frac{n_{ik}(j)}{n_{ik}} \quad (1)$$

where n_{ik} is the number of topological shortest paths between the source-sink nodes and $n_{ik}(j)$ is the number of source-sink shortest paths that pass through node j. The computation can be accomplished using Floyd's shortest paths algorithm for source-sink pair of nodes [Floyd, 1962]. Assuming that the flow is routed through the most direct path, the betweenness of a node gives an approximation of the amount of information flowing through it [Albert et al. 2004], and for this

reason the alternative term load is used to denote it. Likewise, the load, L_{ij}, or amount of flow passing through an edge, is measured by the edge betweenness [Girvan and Newman, 2002]. Node/edge betweenness measures the influence of a node/edge with respect to the flow of information in the network, especially in cases where the flow of information follows the available source-sink shortest path [Albert et al., 2004].

In order to assess the status of a component, its load is compared with the component capacity, i.e. the maximum load that it can process. The capacity is limited by technological constraints and economic factors. The capacity of node *j* is dimensioned proportionally to its nominal load L_j at which it is designed to operate, $C_j = (1+\alpha)L_j$. Likewise, the capacity of link *ij* is dimensioned proportionally to its nominal load L_{ij} at which it is designed to operate, $C_{ij} = (1+\alpha)L_{ij}$, where $\alpha > 0$ is the tolerance parameter of the network system. This parameter can be regarded as an operating margin allowing safe operations of the component under possible load increments. When $\alpha = 0$, the system is working at its limit capacity, its operating margin being null: any further load added to a component would result in its failure and, possibly, in the propagation of a cascading failure involving a large part of the system.

When a component fails, it ceases to provide its service; thus, it is considered inactive, i.e., as removed from the system. This leads to a redistribution of the shortest paths in the network and, consequently, to a change in the loads of the active components. If the load on a component increases beyond its capacity upon redistribution of the shortest paths, the component fails and a new redistribution follows. This iterative process results in a cascade of successive failures. Therefore, the cascading failure dynamics is function of both edges and nodes states. This adds to the reference abstract model [Batagelj, 1994; Motter and Lai, 2002; Albert et al., 2004; Newman and Girvan, 2004; Latora and Marchiori, 2005; Duenas-Osorio and Vemuru, 2009; Zio and Sansavini, 2010], that does not account for the loads on the edges.

In this work, the effects of cascading failures is summarized by two indicators, the connectivity loss, C_L, and the cascade size, *S*. The former quantifies the decrease of the ability of sink nodes to receive flow from source nodes; its calculation relies on the topological structure of the network and the available "least-resistance" pathways:

$$C_L = 1 - \frac{1}{N_D}\sum_{i=1}^{N_D}\frac{N_G^i}{N_G} \tag{1}$$

where N_G and N_D represent the numbers of source and sink nodes in the unperturbed state of the network system, and N_G^i represents the number of source nodes able to supply flow to sink node *i* after failures take place [Albert et al. 2004; Duenas-Osorio and Vemuru, 2009].

While the failure of lines only contributes to the further propagation of the cascade through load redirection, the failure of nodes implies also the inability to provide flow to certain areas of the network. Therefore, the disruption caused by the cascade of failures is quantified by the number of inactive nodes, through *S*, and by the inability of source nodes to provide flow to sink nodes, through C_L.

3. Network protection strategies

Prior to the development of the NP strategies, we introduce the attack/failure scenario whose consequences have to be minimized.

Similar to the network worst-case interdiction contingency [Salmeron et al., 2009], we consider the attack/failure that maximizes the damage from a cascading process triggered by the removal of a single component. This is consistent both with an optimal attack strategy that minimizes the damaging resources and with the worst-case random failure of a single component. Intuitively, two situations are expected. If prior to its removal the component is operating at a relatively small load, its removal will not cause major changes in the balance of loads, and subsequent over load failures are unlikely. However, if the load of the component is relatively large, its removal is likely to affect significantly the loads of other neighboring components, and possibly to start a sequence of overloads impacting on the whole system. Furthermore, the following behavior is expected [Motter and Lai, 2002]: global cascades occur if the network exhibits a highly heterogeneous distribution of loads, and the removed component is among those with highest loads; otherwise, cascades are not expected. Therefore, to define the scenario that triggers the cascade of failures, we identify the component whose removal yields the largest disruption in the network. This is equivalent to identifying the worst NI scenario that is produced by damaging one single component.

Unlike the common NI practice [Salmeron et al., 2004, Bier et al., 2007, Salmeron et al., 2009], here the results of NI are not subsequently employed to harden the identified critical components; rather, NP by line switching is performed.

Specifically, NP is modeled as an operator intervention aiming at minimizing the effects of the cascade failure propagation by disconnecting lines immediately after a cascade is triggered. In other words, line switching is used as corrective measure, to prevent the propagation of the cascade of overloads. This control technique has here been deployed within the devised modeling framework which abstracts the physical properties of the network system, and assumes that flow is routed through the source-sink shortest paths in the network. Due to the rapid unfolding of a cascade, we assume that the protection intervention takes place only once after the cascade is triggered: no further actions to correct the effects of this only protective action are taken.

In order to highlight the benefits of the optimized NP, we present and investigate several protection strategies:

- *Single-line switching*

  First, we consider a “blind” protection strategy consisting in opening one single line to prevent failure propagation. This scenario implies that the operator is endowed by enough time and/or resources to perform the switch off of a single line. We aim at identifying the line whose disconnection hinders the most the cascade propagation, yielding the best improvement in terms of C_L and S.

- *Multiple-line switching*

  A more realistic protection intervention assumes that the operator is given time, resources and knowledge enough to be able to switch off more than just one line. Then, the problem arises of what is the best set of lines whose disconnection hinders the most the cascade propagation. This issue is not trivial in that the intentional disconnection of lines can worsen the effects of the cascade in the same way as propagation of failures does. As in the single-line protection strategy of Section 3.1, the operator intervention occurs immediately after the cascading failure is triggered.

Two complementary approaches to NP are suggested in the literature [Talukdar et al., 2003]. The first aims at minimizing the effects of cascading failures at the global system level. A measure of network disruption is identified and the operator acts on the network by switching off lines in order to minimize it. This global protection strategy points to the development of an invulnerable network. On the other hand, it fails identifying those critical locations or essential services to which flow of information has to be guaranteed under any contingency. Therefore, a second, local perspective on NP is directed towards assuring the continuation of identified essential locations, services and missions even after the network has failed. In light of these dual perspectives on NP, we devise three strategies that differ in the objectives of the optimization.

As previously explained, the two indicators, C_L and *S* can be used to quantify the effects of cascading failures. Nevertheless, there is a strong correlation between them in the sense that the failure of nodes, which is equivalent to an increase of *S*, produces also an increase of C_L. Similarly, we expect that an improvement in C_L by NP will produce an improvement of *S*. Due to the fact that it is intrinsically easier to reduce *S* than C_L, we set the minimization of C_L as the sole objective of NP optimization.

The global protection optimization seeks interventions that minimize the objective function $\mathrm{f}(\mathbf{x}) = \min_{\mathbf{x}} C_L(\mathbf{x})$, i.e. the connectivity loss of the network configuration $\mathbf{x} = \left\{ x_j \,\middle|\, x_j \in \{0,1\},\ j = 1,...,K \right\}$, where $x_j = 1$ if line *j* is operating, or 0 otherwise.

On the other hand, the local optimization searches for the optimal intervention in terms of the line switching set $\mathbf{x}$ that minimizes the connectivity loss C_{L_A} of a specific area A identified as of particular importance, $\mathrm{f}(\mathbf{x}) = \min_{\mathbf{x}} C_{L_A}(\mathbf{x})$. In this framework of the problem, C_{L_A} measures the ability of the sink nodes *j* within the area A to receive flow from any source in the whole network:

$$C_{L_A} = 1 - \frac{1}{N_{D_A}} \sum_{i=1}^{N_{D_A}} \frac{N_G^i}{N_G}, \tag{2}$$

where N_G represents the number of the source nodes at the unperturbed state of the network, N_{D_A} represents the number of sink nodes within the area A at the unperturbed state of the network, and N_G^i represents the number of source nodes able to supply flow to sink node *i* in area A, after failures take place.

In order to fully take advantage of both perspectives on NP, we look into a third "hybrid" protection strategy that finds the set of lines to be switched-off, $\mathbf{x}$, that minimize both the connectivity loss of a pre-identified area A, $C_{L_A}(\mathbf{x})$, and the connectivity loss of the whole network, $C_L(\mathbf{x})$. This originates a multi-objective (MO) optimization problem.

The optimizations are carried out by a MBDE algorithm, that uses binary variables to characterize the line switching decisions. The developed optimization algorithm is detailed in Section 4.

The algorithm for simulating the combined effects of cascading failures and protection strategies (hereafter optimally implemented) proceeds in successive stages as follows.

Initially, all components, N nodes and K lines, are characterized by initial loads L_i and L_{ij}, respectively, and maximum capacities, C_i and C_{ij}, respectively.

0. The initiating event occurs, i.e. the failure of the most critical component, which is removed from the network. This triggers the cascading failure. Each component that is operating is tested for failure: for $i = 1, ..., N$, if node i is working and $L_i > C_i$ then node i fails; if link ij is working and $L_{ij} > C_{ij}$ then link ij fails.

1. The operator intervenes by disconnecting a set of lines, in order to limit the cascade failure effects, expressed by the objective functions relative to the selected optimization strategy (global, local or hybrid). The MBDE optimization algorithm returns the most appropriate network configuration that minimizes the objective functions at the end of the current step $t = 1$.

2. The components loads are re-distributed taking into account the new, protected network topology. Each component that is operating is tested for failure: for i =1,..., N, if node i is working and $L_i > C_i$ then node i fails; if link ij is working and $L_{ij} > C_{ij}$ then link ij fails.

3. The stage counter t is incremented by 1 and the algorithm is returned to step 2.

The algorithm stops when no more working nodes fail.

4. Modified binary differential evolution algorithm

A binary DE [Wang et al., 2010] is used for optimizing a multiple-line switching strategy.

DE has been originally developed as a population-based global optimization algorithm for real-valued optimization problems [Storn and Price, 1995]. The revolutionary idea of DE lies in the perturbation of the current population: this is obtained by adding to a chromosome the weighted difference between two others randomly selected from the population. The initial population is randomly generated by sampling values uniformly distributed between the lower and upper bounds of each of the decision variables. Three evolutionary operations, i.e., mutation, crossover and selection are used to update the population.

During the first operation, the mutated individual $\mathbf{v}_i$, called noisy vector, is generated according to the following equation

$$\mathbf{v}_i^{t+1} = \mathbf{x}_{r_1}^t + F \cdot (\mathbf{x}_{r_2}^t - \mathbf{x}_{r_3}^t) \tag{3}$$

where F, a positive real constant, is the scaling factor, t is the index of generation and $\mathbf{x}_{r_1}^t$, $\mathbf{x}_{r_2}^t$ and $\mathbf{x}_{r_3}^t$ are three randomly chosen individuals, i.e., target vectors, with indexes $r_1 \neq r_2 \neq r_3 \neq i$.

After mutation, the noisy vector is further modified by the crossover process, in which the noisy and target vectors are mixed according to some rule to create the trial vector $\mathbf{u}_i$. The trial vector inherits from the noisy and the target vectors different pieces of chromosome, as regulated by the crossover rate CR. The commonly used binomial crossover is defined as:

$$\mathbf{u}_{ji}^{t+1} = \begin{cases} \mathbf{v}_{ji}^{t+1}, \text{ if } U(0,1] \le CR \text{ or } j = \text{irand}(NP) \\ \mathbf{x}_{ji}^{t}, \text{ if } U(0,1] > CR \text{ and } j \ne \text{irand}(NP) \end{cases} \quad (4)$$
$$\forall j \in \{1,2,...,K\}$$

where $U(0,1]$ is a uniform continuous random value $\in [0,1]$, $irand(NP)$ is a uniform discrete random number in the set $\in \{1,2,...,NP\}$, NP is the population size, j is the index of the dimensionality and K is the length of the chromosome.

The selection operator is defined as:

$$\mathbf{x}_{i}^{t+1} = \begin{cases} \mathbf{u}_{i}^{t+1}, \text{ if } \text{f}(\mathbf{u}_{i}^{t+1}) < \text{f}(\mathbf{x}_{i}^{t}) \\ \mathbf{x}_{i}^{t}, \text{ otherwise} \end{cases} \quad (5)$$
$$\forall i \in \{1,2,...,NP\}$$

Referring to a single objective (SO) minimization, if the fitness value of the trial individual is better than the target one, it replaces the target individual; otherwise, the target individual is preserved in the next generation. This criterion ensures that the next generation is better or at least equal to the previous one.

DE can tackle MO optimization problems in different ways [Babu et al., 2007]. In this work, we adopted an efficient MO differential evolution (MODE) version [Babu et al., 2007] that inherits the strength of the selection process thought for SO optimization: each trial vector is compared only with its target from which it inherits some variables, and, if the trial dominates the target vector, it takes its place in the population for the next generation; otherwise the target vector survives. The selection procedure, applied with its original purpose but under a MO frame of dominance [Babu et al., 2007], allows saving considerable time because no ranking of the population is adopted and a dominated comparison is made only NP times each generation [Zio and Viadana, 2011].

Of course, without any ranking, the selection of the chromosomes for reproduction can only be random. The stopping criteria usually adopted in MO optimization is the reaching of a defined number of maximum generations. Thanks to the goodness of the reproduction ability and exploration of DE, the Pareto frontier of optimality [Babu et al., 2007] is achieved by a large fraction of the population.

Two indicators of the performances of MO optimization schemes are the computation time and the fraction of non-dominated solutions found in the last population: the larger the fraction is, the higher is the ability to get to the Pareto frontier.

In order to solve discrete optimization problems, MBDE uses a bit-string framework: each individual is represented as a vector and denoted as $\mathbf{px}_i = \{\mathbf{px}_{ij} \,|\, \mathbf{px}_{ij} \in \{0,1\};\ i = 1,\ 2,...,NP,\ j = 1,...,K\}$ where NP is the population size and K is the dimensionality of the solutions. MBDE preserves the updating strategy of the standard DE, including the mutation, crossover and selection operators. Since the standard mutant operator generates real-coded vectors and not binary-coded strings, an effective probability estimator operator is integrated into the mutant operator [Wang et al., 2010]:

$$P(\mathbf{px}_{ij}^{t}) = \frac{1}{1+e^{\frac{2\cdot b\cdot[\mathbf{px}_{r1,j}^{t}+F\cdot(\mathbf{px}_{r2,j}^{t}-\mathbf{px}_{r3,j}^{t})-0.5]}{1+2\cdot F}}} \tag{6}$$

where b is a positive real constant, often set to values around 6, F is the scaling factor just the same as that of the standard DE, $\mathbf{px}_{r1,j}^{t}$, $\mathbf{px}_{r2,j}^{t}$ and $\mathbf{px}_{r3,j}^{t}$ are the j-th bits of the three randomly chosen individuals at generation t.

The decision variable vector is composed of K elements corresponding to the network lines; each element contains 1 if the corresponding line is to be switched-off, 0 otherwise. The optimization is SO for the global and local protection strategies, and MO for the "hybrid" protection strategy.

5. Results and discussion

We illustrate the dynamics of the network model and its optimal NP protection by the framework of Sections 3 and 4, taking for reference the topology of a realistic network system, i.e. the 380 kV Italian power transmission network (Figure 1).

It is understood that the outcome of the vulnerability analysis of an infrastructure such as the electricity network here considered significantly depends on the modeling paradigm and on the metrics that are used to quantify the response of the network to attacks and failures. In this respect, [Hineset al., 2010] have compared three vulnerability measures, respectively, two topological measures, i.e. path length and C_L, and one functional measure, i.e. blackout size for the analysis of an electric power grid. The topological measures quantify the effects of the disconnection of groups of components on the network structure irrespective of flow rerouting. On the contrary, the blackout size is the amount of load curtailed in a DC power-flow simulation that incorporates line tripping due to flow limits, generator set-point adjustments and load shedding. Within the embraced frame of work, they found that C_L predicts only the minimum size of the blackout because it does not directly account for cascading failures. Furthermore, the three vulnerability measures provide different rankings for the identified risks. From the path length metric, the removal of components with large betweenness appears to have the greatest impact, while C_L ranks as more dangerous the removal of the most connected nodes. Eventually, from the blackout model, the removal of nodes that transport the largest amount of power appears to contribute most to vulnerability.

Here, we exemplify the proposed methodology with reference to the power transmission network mentioned above, focusing only on its the structure with no further reference on the physical and electrical properties. The 380 kV Italian power transmission network is a branch of a high voltage level transmission, which can be modeled as a network of $N=127$ nodes, i.e. buses ($N_G=30$ source nodes, i.e. generators and $N_D=97$ sink nodes, i.e. distribution substations) and $K=171$ edges, i.e. electrical connections. The generator substations, i.e. hydro and thermal power plants are represented in Figure 1 by squares whereas the distribution substations are represented by circles. As described in Section 2, the load of a component, i.e. nodes and lines, is assumed equal to the total number of shortest paths connecting every source node to every sink node passing through that component. This assumption may not be valid for electrical power grids, where power flows according to physical rules such as Kirchhoff's laws, and load requests. Nevertheless, it serves the purpose of the paper which is to look into the structural properties and apply the NP optimization framework to a complex network of realistic size.



Figure 1. The 380 kV Italian power transmission network [TERNA, 2002; Rosato et al., 2007]

Figures 2 and 3 show the load distribution on each component when the network operates at nominal conditions. Node 88 and line 104 (the line connecting nodes 75 and 88) handle the largest load in the system, i.e. the largest number of source-sink shortest paths.

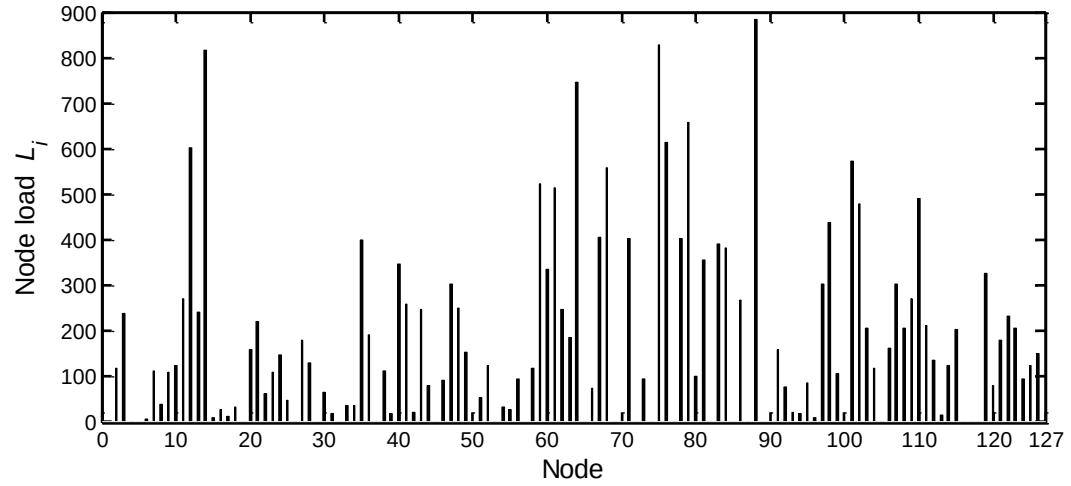


Figure 2. Loads on each node in the unperturbed configuration

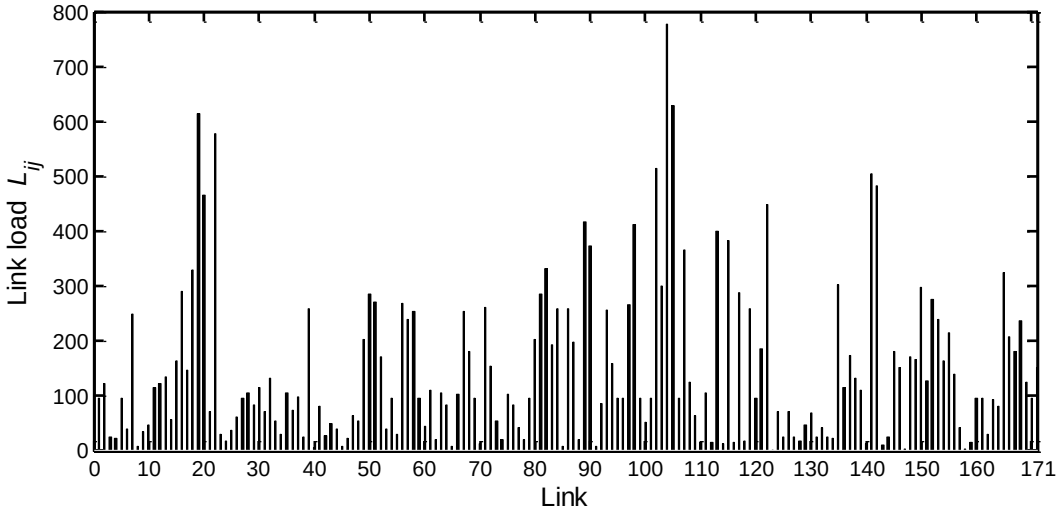


Figure 3. Loads on each line in the unperturbed configuration

The initiating event is identified as described in Section 3. Contrary to what can be supposed, it is found that the largest damages to the network are due to removals of components that are not among the most loaded (Figures 4-7). The removals of nodes 86 and 78 have the largest impacts on the network with respect to both C_L and S. The failure of the most loaded node, i.e. node 88, leads to cascades involving 28 components, compared to 48 components that failed when node 86 triggers the cascade. Also, $C_L = 0.77$ when the system stabilizes if node 88 is removed, but $C_L = 0.94$ when node 78 fails. The criticality of nodes 86 and 78 with respect to cascading failures is due to their position in the network, in proximity of highly loaded nodes.

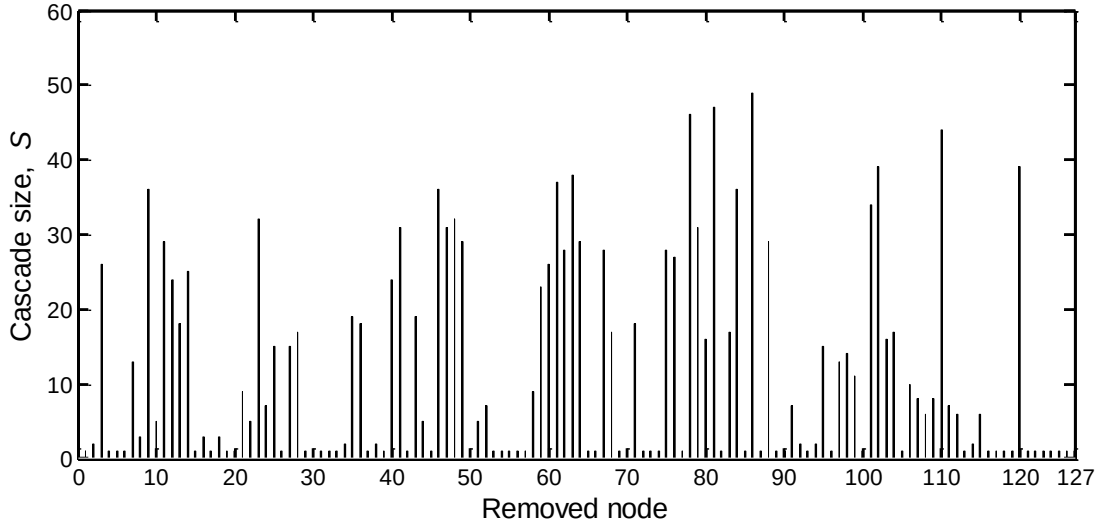


Figure 4. The cascade size, S, caused by the removal of each node (abscissa) in the power transmission system of Figure 1

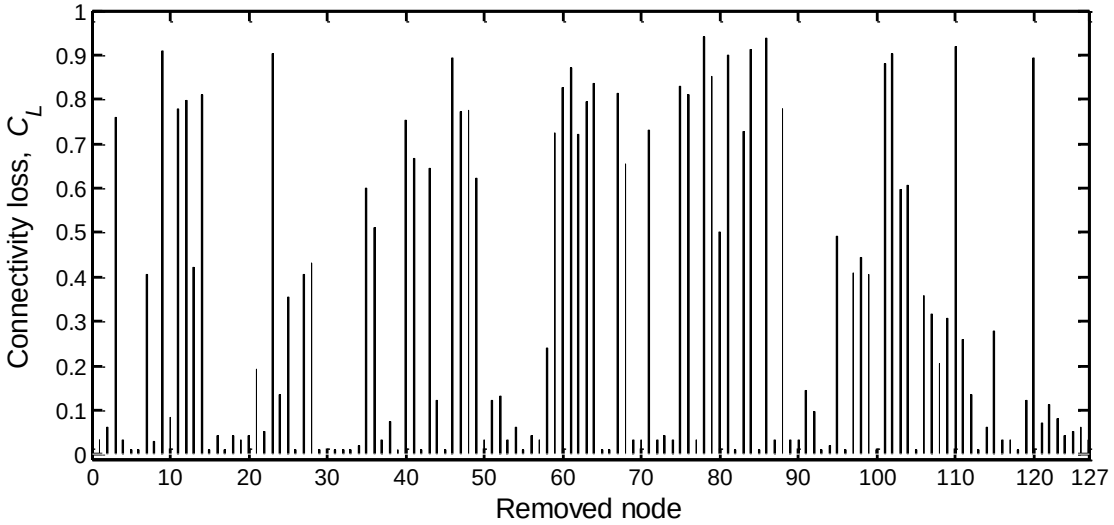


Figure 5. The connectivity loss, C_L, caused by the removal of each node (abscissa) in the power transmission system of Figure 1

In order to identify the worst NI scenario that triggers the cascading failure, the effects of cascading failures are further investigated also with respect to the loss of lines. The removal of link 107 connecting nodes 78 and 81, results in the largest damage in terms of S (57 nodes fail at the end of the cascade failure propagation) and $C_L = 0.96$, while the failure of the most loaded link, i.e. 104, leads to $S = 27$ components and $C_L = 0.71$. Also in this case, the average initial load has little influence on the criticality, whereas the neighbors load and the failure of the connection between node 78 and 81, have a large impact (node 78 was found to be one of the most critical nodes in triggering the cascading failure propagation).

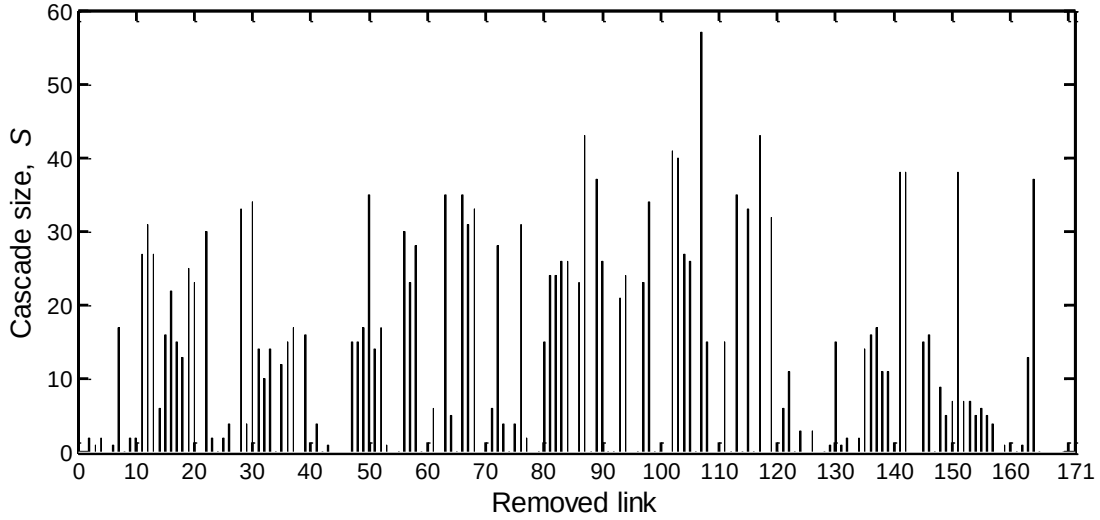


Figure 6. The cascade size, S , caused by the removal of each link (abscissa) in the power transmission system of Figure 1

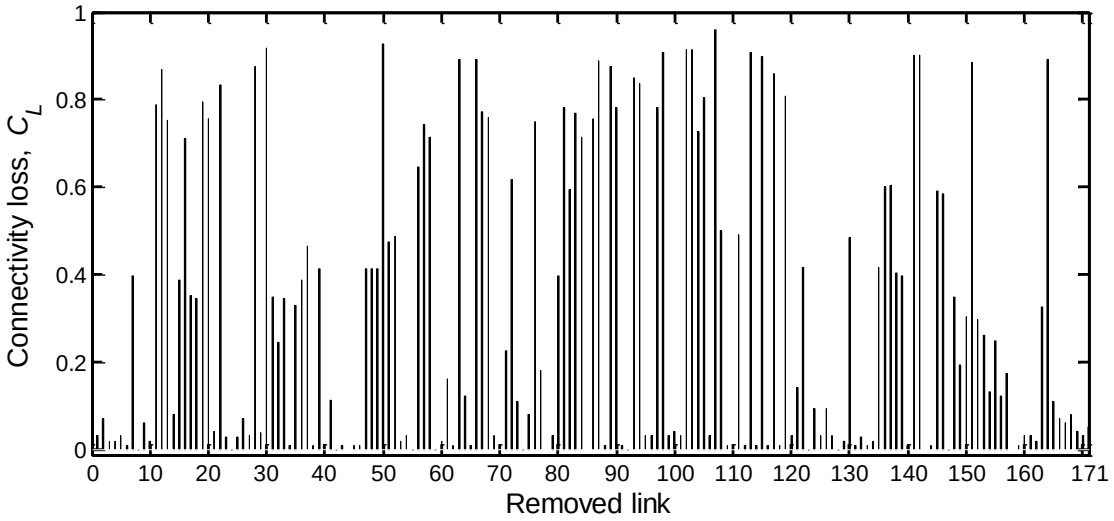


Figure 7. The connectivity loss, C_L , caused by the removal of each link (abscissa) in the power transmission system of Figure 1

The difference between the failure of a node and that of a link lies in the redistribution of the components loads. A major initial damage is obtained after the failure of a node, since this implies also the disconnection of its direct connections. Nevertheless, the redistribution of the shortest paths leads to a small increase of load of a larger number of components. On the other side, the failure of a line produces a larger increase of load of the first order neighbors that further affects the cascade propagation. We observe that, on average, the loss of links results in a more severe damage than that caused by the loss of nodes, at the end of the cascade propagation, both in terms of C_L and S . We therefore identify the disconnection of the transmission line (edge) 107 as the worst-case NI scenario.

5.1 Single-line switching

As we have explained, the cascade propagation is triggered at $t = 0$ by an attack/failure consisting in the disruption of link 107, which produces the loss of six nodes by the end of the computational step. We aim at reducing the effects of the cascade of failures in the network through the application at $t = 1$ of the single-line switching strategy described in Section 3.

Figures 8 and 9 show the effect of single-line switching as compared to not protecting the network, in terms of both C_L and S.

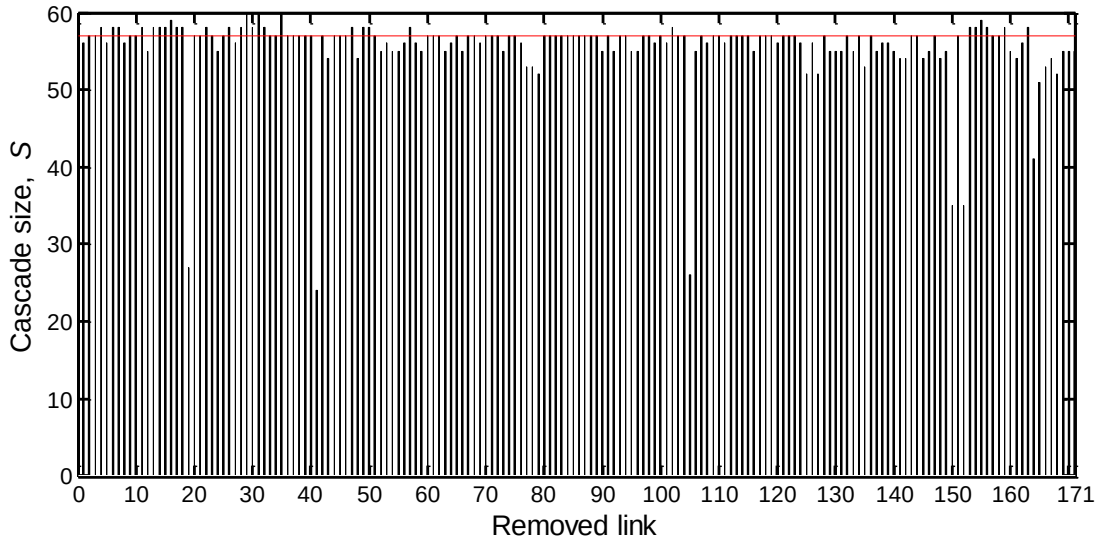


Figure 8. The cascade size, S, resulting from the initial attack on the line 107 followed by the operator intervention of opening a line (abscissa). Horizontal line $S = 57$ represents the reference cascade size, i.e. obtained without any further intervention after the attack

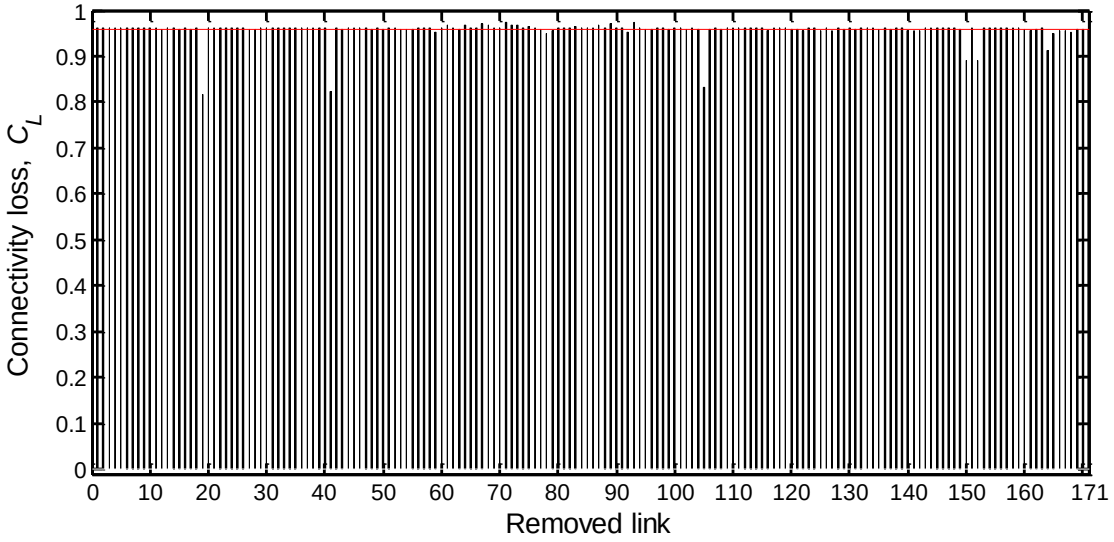


Figure 9. The connectivity loss, C_L, resulting from the initial attack on line 107 followed by the operator intervention of opening a line (abscissa). Horizontal line $C_L = 0.96$ represents the reference connectivity loss, i.e. obtained without any further intervention after the attack

The following observations can be drawn from Figures 8 and 9: i) the disconnection of a line as a corrective measure mostly reduces S but in some cases it enhances it, as for the disconnection of lines 28, 30, 35; this is due to the increase of node loads after the redistribution of shortest paths, following the removal of a link; ii) with few exceptions (lines 19, 41, 89), C_L remains mostly unchanged upon intervention that disconnects a single line; this indicates that the identified best interdiction scenario causes severe network disruptions before any intervention is made; iii) while S can be reduced to a maximum of 60%, C_L can be barely reduced by 15% of its value when no intervention occurs: this is due to the irreversible partition of the network into two islands (the north and the south halves) with the associated irreversible loss of north-south source-sink connections. Then, this protection strategy fails to maintain a satisfactory level of connectivity between source and sink nodes, although it improves the survivability of the network components. These observations suggest the need of a more effective protection strategy, capable of decreasing the effects of connectivity disruption of cascading failures. Since C_L and S are directly related, we expect that an improvement in the loss of connectivity will lead to a decrease of S. We therefore propose an optimization scheme for protecting the network that aims at minimizing C_L.

5.2. Multiple-line switching

We assume that the protection intervention takes place only once at $t=1$ after the cascade is triggered at $t=0$. The attack/failure of the transmission line 107, i.e. the worst-case NI scenario, produces the loss of six nodes before any operator intervention can occur. This Section presents the results obtained by combining the protection strategies of Section 3 and the MBDE of Section 4. The simulation parameters used in the optimization schemes are summarized in Table 1.

Table 1. The parameters of the MBDE algorithm

MBDE parameters	
Population size *NP*	40
Dimensionality of solutions *K*	171
Crossover rate *CR*	0.8
Scaling factor *F*	0.2
Minimum fitness error	10^{-4}
Maximum number of generation	1500

5.2.1 Global protection

Figure 10 presents the evolution of the cascade after the initial failure, without any intervention (dotted line) and with the intervention of switching off the optimal set of lines, both in terms of S (left graph) and C_L (right graph). The results obtained at the end of the optimization algorithm are summarized in Table 2.

The effects of the optimal intervention in terms of line switching can be evinced by comparing the evolutions in Figure 10. The optimal line switching intervention at $t=1$ reduces S and C_L by 87.7% and by 34.6%, respectively. The failures keep propagating in the network and the cascade

ends at $t=3$. The results obtained when the system is stabilized are satisfactory: S is reduced from 57 nodes to 10 nodes, while C_L is improved by approximately 21%. There are four nodes that fail after the operator intervenes according to the protection strategy, i.e. nodes 7, 9, 10 and 20, located in two different geographical regions of northern Italy (Figure 1).

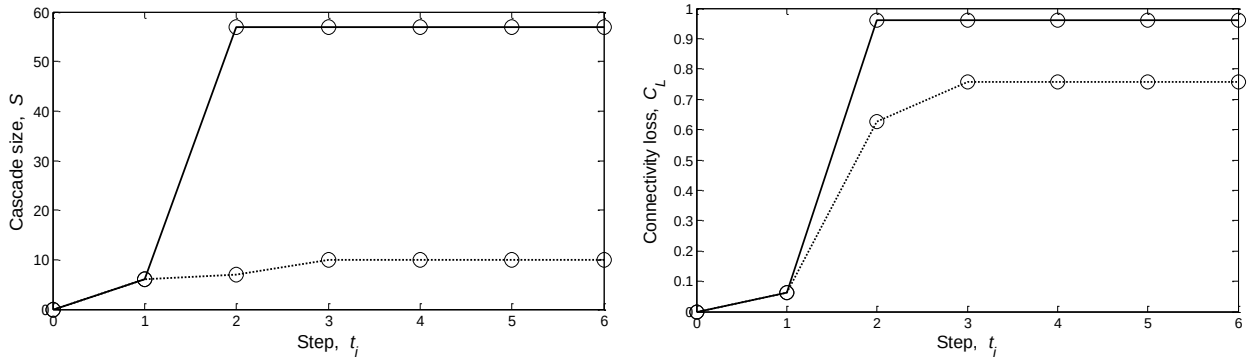


Figure 10. The cascade evolution in terms of cascade size, S, and connectivity loss, C_L, after the failure of line 107 and with no intervention at $t=1$ (solid lines) or optimal operator intervention at $t=1$ (dotted lines)

Table 2. Best optimal global switching scheme

Number of lines	Optimal line switching scheme	Connectivity loss, C_L	
		computational time $t=1$	end of cascade
27	2-8, 5-6, 14-73, 15-17, 17-18, 24-28, 25-27, 28-30, 32-35, 34-38, 41-64, 41-66, 43-46, 48-53, 51-54, 55-56, 79-81, 89-91, 91-92, 92-93, 96-98, 97-103, 103-104, 110-111, 113-120, 115-118, 121-123	0.608	0.758

These improvements have been achieved by disabling 27 lines, i.e. 21% of the network connections (Table 2, column 2). For most of the network systems [Arroyo and Ferdandez, 2009], this represents a feasible number of lines to be switched-off and it is consistent with the size of other protection strategies reported in the literature. As an example, in [Arroyo and Fernandez, 2009] a strategy is suggested that involves the switching-off of 24% of the network lines. For particular complex network systems such as electrical networks, for which the proposed protection scheme is nearly equivalent to a black-out, a multiobjective optimization aimed also at reducing the number of lines to be switched-off could be addressed. The optimal set of lines identified in the protection strategy is represented in Figure 11. The lines are spread over the entire network with a major concentration in the northern part. By adopting this protection strategy, the operator intervention maintains a good level of working components with acceptable C_L.

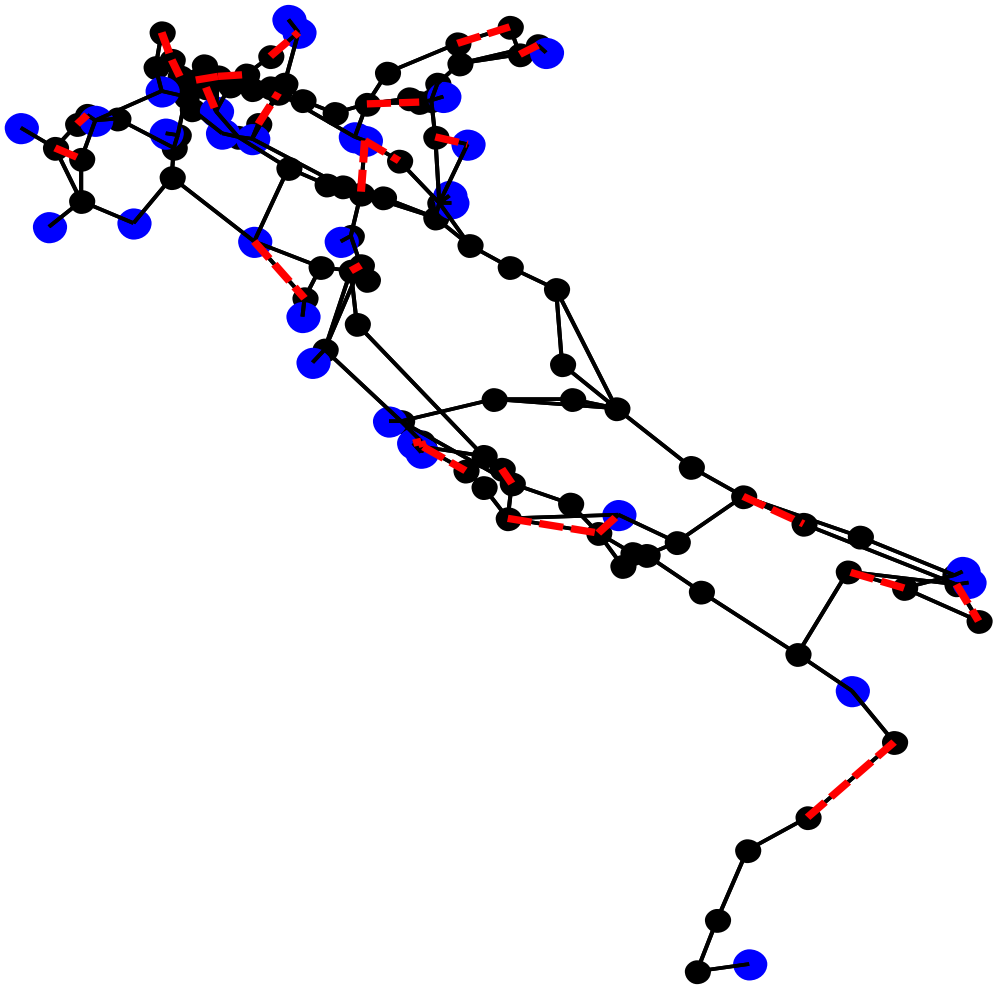


Figure 11. The dashdotted lines in this graphic representation of the network are the optimal set of 27 edges to be switched-off to optimally contain the failure cascade, in the global optimization approach to protection

5.2.2 Local protection

Since the region of Lombardy, situated in the central part of the northern Italy, includes the largest number of distribution substations, i.e. sink nodes in the network of Figure 1, i.e. 21 sink nodes, our local protection strategy will focus on the minimization of the loss of connectivity of this specific area, C_{L_A} .

The results obtained by the MBDE optimization are summarized in Table 3. The operator intervention entails the disconnection of 41 lines. The effects of the operator optimal intervention in terms of line switching can be evinced by comparing the evolutions in Figure 12. The immediate aftermath of the protection strategy is the reduction of the local-area average C_{L_A} from 0.979 to 0.551 at $t = 2$. The modest decrease of $C_{L_A} = 0.823$ (by 16% of the value obtained with no intervention $C_{L_A} = 0.979$) at the end of the cascade, is conditioned by the loss of a large number of paths connecting long-distant source nodes, while the nearby ones keep supplying the sink nodes within the region of interest. Indeed, the protection strategy entails a small number of lines to be switched-off in the northern regions, while the majority of lines belonging to the identified optimal

set are located in the other areas of the network. It is worth noticing that even if the total number of failures at the end of the propagation is the same as in the global strategy, i.e. $S = 10$, in this case the sink node 20 located in the northern side of Figure 1 is protected through line switching; this validates the efficiency of the local protection strategy.

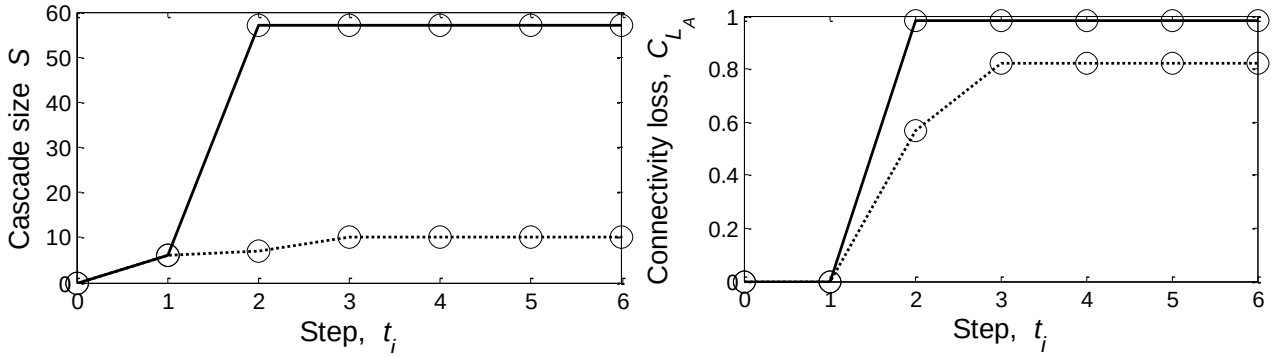


Figure 12. The cascade evolution in terms of cascade size, *S*, and local-area connectivity loss, C_{L_A}, after the failure of line 107 and with no intervention at $t = 1$ (solid lines) or optimal operator intervention at $t = 1$ (dotted lines)

5.2.3 "Hybrid" protection

As explained in Section 3, the "hybrid" multiple-line switching protection strategy aims at minimizing both the overall network connectivity loss, C_L and the connectivity loss of the region of Lombardy, C_{L_A}, within a multi-objective optimization framework.

The results obtained are summarized in the last 3 rows of Table 3. Five MBDE optimization runs were performed, starting from different initial random populations. The Pareto frontier, obtained by selecting the non-dominated solutions among those reached in the different runs is represented in Figure 13. The fraction of dominant solutions is 0.8; of these, 32 are present in the last population.

The CPU time was 4300 s on a Pentium(R) Dual-Core 2.7 GHz PC with 3 GB RAM.

This protection strategy yields the best results. We are able to reduce both values of connectivity loss, C_L and C_{L_A}, near their minimum values obtained in the global and local protection strategies. A small variation can be observed regarding the total number of lines to be switched-off, which remains always lower than in the local strategy, and the final size of the cascade failure propagation.

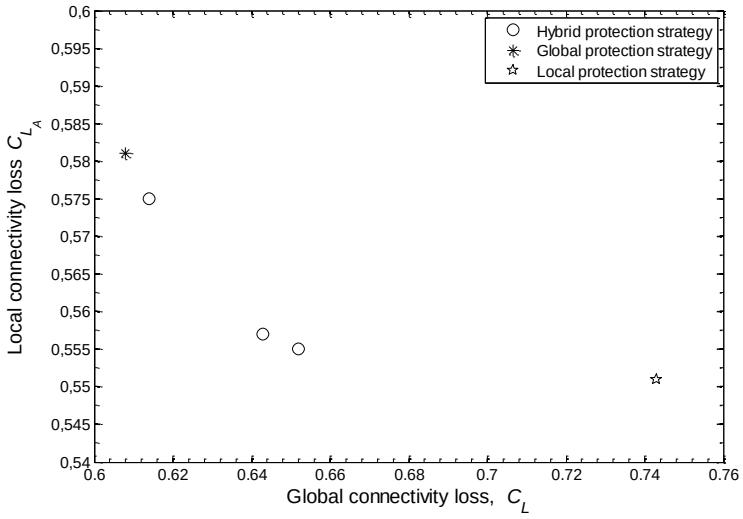
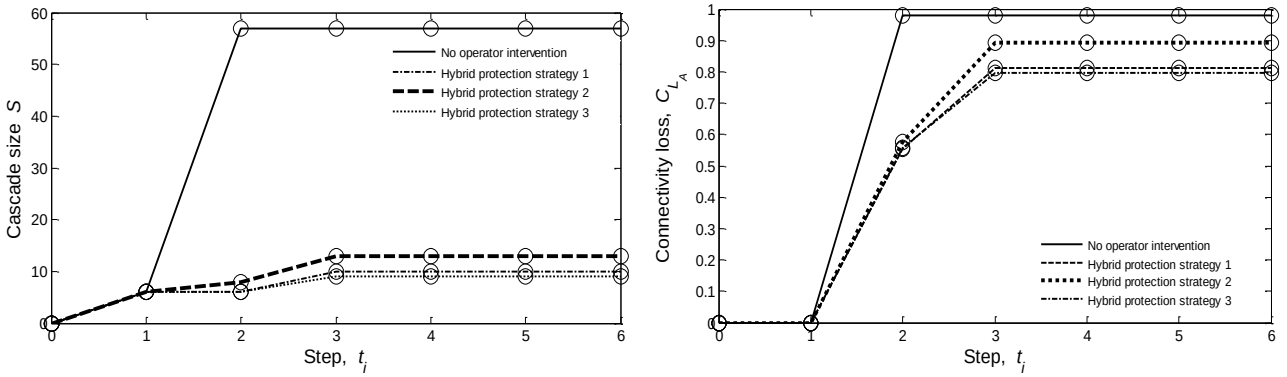


Figure 13. The Pareto frontier identified at $t=1$ after the multiple-line switching optimal operator intervention

The effects of the operator optimal intervention in terms of line switching can be evinced by comparing the evolutions in Figure 14. The first NP strategy identified within the "hybrid" protection strategy presents the best performances with respect to the local parameters, i.e. C_{L_A} after the protection strategy, at $t=2$, and at the end of the cascade failure, i.e. at the end of the cascade, maintaining *S* at the same level of the global and local strategies. The results obtained by the second "hybrid" strategies are satisfactory with respect to the number of lines to be switched-off and also with respect to C_L and C_{L_A}, but entail an increase of S. The best strategy is the third one, that even if it fails to minimize the immediate aftermath of the protection strategy, it achieves an improvement of all indicators at the end of the cascade propagation.



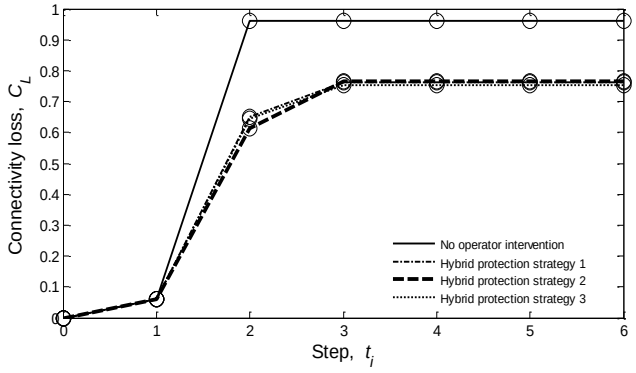


Figure 14. The cascade evolution in terms of cascade size, *S*, and connectivity loss, C_L and C_{L_A}, after the failure of line 107 and with no intervention at $t=1$ (solid lines) or with optimal operator intervention at $t=1$ (dashed and dotted lines for the three hybrid strategies resulting from the MO optimization)

It is interesting to note that in all optimal strategies there are three common nodes that always fail after the protection intervention, i.e. nodes 7, 9 and 10, all situated in the northwestern region (Figure 1). Following this observation, a more accurate vulnerability analysis involving these nodes could be performed and a decision regarding the protection and the strengthening of them could be taken. This would lead to a further reduction of the number of nodes failed and the cascade failure propagation could be avoided.

Table 3. Comparison of different protection strategies (dark-shaded areas denote the results obtained at $t=2$, light-shaded areas denote the results obtained at the end of the cascade after the operator intervention)

Protection strategy			C_L		C_{L_A}		Number of switched-off lines	Cascade size, *S*
			computational time $t=2$	end of cascade	computational time $t=2$	end of cascade		
No operator intervention			0.959	0.959	0.979	0.979	-	57
Single-line switching			0.810	0.818	0.914	0.932	1	27
Multiple-line switching	Global protection		0.608	0.758	0.581	0.832	27	10
	Local protection		0.743	0.844	0.551	0.823	41	10
	Hybrid protection	1	0.652	0.762	0.555	0.811	31	10
		2	0.614	0.765	0.575	0.894	26	13
		3	0.643	0.753	0.557	0.797	30	9

6. Conclusions

In this paper, we embraced a complex network perspective on the problem of optimal protection of network systems. We extended a previously developed model for cascading failures propagation

based on complex network theory, and embedded it in an original MBDE scheme of optimization which considers both global and local effects on the network.

Optimal protection strategies involving line switching have been identified such as to limit the cascade failure consequences. Numerical results obtained by application of the MBDE optimization methodology on a mid-size network have proved both feasible and satisfactory. The suggested protection strategy, i.e. the optimal set of lines to be switched-off, proved efficient in limiting the cascading failure consequences of the worst-case interdiction scenario. Nonetheless, we observed that the disconnection of a single line as a corrective measure may increase the extent of a cascade in some cases. We conclude that a hybrid protection strategy would combine the benefits of the global network protection and of the predefined local area protection. Therefore, the results of this work foster the use of a hybrid approach to obtain the optimal network protection.

The abstract modeling approach undertaken for analyzing the system aims at characterizing the topology of network systems for identifying critical parts and selecting optimal protection strategies. However, given the somewhat abstract level of the modeling supporting complex network analysis, the insights gained with respect to the vulnerable areas in the system (first findings) may not be clear-cut, and additional vulnerabilities may still be expected, and more detailed information about the system and its operating environment needed. Then, for practical uses the analysis can serve for guiding more detailed approaches that include operational aspects related to the specific system. For example, for a power system it would be necessary to account for: the line impedances and Kirchhoff's laws in assessing the power flows from the generators to the loads, the fact that the line capacities are engineered to accommodate the usual patterns of line flows, the effects of automatic protection, power flow redistribution after transients and after re-dispatch of generation and shedding of load. Further, the use of line switching, here taken only as an example of protection measure, must be carefully considered in practice: as observed in our results, the action of switching off transmission lines during a failure could itself worsen the behavior of the system.

In this direction, introduction of physical characteristics into abstract modeling approaches is envisaged. The introduction must be suitable to bridge the modeling to reality, without over-complicating the model that remains appealing if it requires minimum information and provides prompt results about network vulnerability.

In this respect, this work just takes the preliminary step of framing the complex network perspective on the problem of optimal protection of network systems. Future research steps will consider the extension of the abstract model of cascading failures “beyond network abstraction” to incorporate physical properties of the specific systems.

Acknowledgements

This work was funded by the Foundation pour une Culture de Securite Industrielle of Toulouse, France, under the research contract AO2006–01.

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