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Finite Dimension Wyner-Ziv Lattice Coding for Two-Way Relay Channel

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Abstract—Two-way relay channel (TWRC) models a cooperative communication situation performing duplex transmission via a relay station. For this channel, we have shown previously that a lattice-based physical layer network coding strategy achieves, at the limit of arbitrarily large dimension, the same rate as that offered by the random coding-based regular compress-and-forward. In this paper, we investigate a practical coding scheme using finite dimension lattices and offering a reasonable performance-complexity trade-off. The algorithm relies on lattice-based quantization for Wyner-Ziv coding. We characterize the rate region allowed by our coding scheme, discuss the design criteria, and illustrate our results with some numerical examples.

Keywords: TWRC, compress and forward, Wyner-Ziv, lattice codes, finite dimension

I. INTRODUCTION

The two way relaying problem where two communicating nodes want to exchange information via a relay is encountered in various wireless communication scenarios: ad-hoc networks, range extension for cellular and local networks ... While network level routing is the standard option to this problem, it has been shown that network coding (NC) strategies provide better performance by leveraging the side information that is available in each node. In fact, NC allows to improve the rates by combining raw bits or packets at the network layer. The capacity of the system can be further improved when NC is applied to the physical layer. It takes advantage of the linear superposition properties of the wireless channel in order to turn interference nuisance into useful signal [1]. In this context, we consider a physical network coding (PNC) strategy where the overall communication takes two phases, namely a Multiple Access (MAC) phase and a Broadcast (BC) phase.

Various strategies have been proposed for TWRC. Amplify and Forward [2], Decode and Forward (DF) [3], and Compress and Forward. The latter has attracted particular attention since it offers a good compromise between processing complexity at the relay and noise amplification. CF for TWRC [4] follows the same strategy of CF schemes for the relay channel [5]. Performance bounds of this scheme have been investigated in [6], [7], [8]. It has been shown that for specific channel conditions, specially symmetric channels, CF outperforms the other relaying schemes for high SNR regimes. In the aforementioned references, the derivation of the achievable rate regions has employed high dimension assumptions and random coding approach which is impractical for real systems. Interestingly, structured codes have been found to be more advantageous in practical settings thanks to their reduced complexity in encoding and decoding [9]. It has been shown in [10] that for an Additive White Gaussian Noise (AWGN) channel, lattice codes can achieve the Shannon capacity for Gaussian point-to-point communication. Based on this result, lattice codes have been extended to TWRC scenario in [11] and [12] as follows : the transmitters employ nested lattices as codebooks, and the relay decodes a modulo-lattice sum of the transmitted codewords from the received signal in order to emulate a XOR operation at the packet level. All nodes (transmitters and relay) are constrained to transmit with the same power and consequently they use the same lattice codebook. In both schemes, the relay follows a DF strategy since it decodes a function of the transmitted lattice codewords. In this paper, we design a new relaying scheme for TWRC based on CF strategy where the relay only compresses the received signal from both nodes based on a knowledge of their transmit power and the channel gain modules. Unlike [11] and [12], our scheme employs lattice encoding only by the relay and is compatible with arbitrary transmit powers and channel gains.

In the MAC phase of our scheme, the communicating nodes send simultaneously their messages and the relay receives a mixture of the transmitted signals. The relay considers this mixture as a source which will be compressed and sent during the BC phase. Taking into account that each terminal has a partial knowledge of this source (side information), the BC phase is equivalent to a Wyner-Ziv (WZ) compression setting with two decoders having a piece of side information each. A lattice based lossy compression is employed to help each user generate a local distorted version of the source. The proposed scheme is based on lattice quantization introduced in [13] and which we extend to the TWRC case. In [14], we have showed that with infinite dimension lattices, this scheme achieves the same rates as the random coding compress and forward strategy. With finite dimension lattices, the decoding error probability cannot be arbitrarily small. Based on this observation, we derive, in this paper, achievable rate regions by considering non vanishing yet constrained decoding error probabilities. The rest of the paper is organized as follows. In
section II, we introduce our system model. In section III and IV, we propose a new lattice-based Wyner-Ziv Coding scheme and we derive its achievable rate region for finite dimensions. In section V, we present a numerical implementation of the achievable rates with practical finite dimension lattices. Finally, section VI concludes the paper.

Notations Random variables (r.v.) are indicated by capital letters where the realizations are written in small letters. Vector of r.v. or a sequence of realizations are indicated by bold fonts.

II. SYSTEM MODEL

We consider a Gaussian TWRC in which two nodes $T_1$ and $T_2$ exchange two individual messages $m_1$ and $m_2$, with the help of a relay $R$ as shown in Fig.1. The relay operates in half-duplex mode. The communication takes $n$ channel uses that are split among MAC phase and BC phase with lengths $n_1 = \alpha n$ and $n_2 = (1 - \alpha)n$, $\alpha \in [0, 1]$ respectively. During the MAC phase, node $T_i$, $i = 1, 2$ draws uniformly a message $m_i$ from the set $\mathcal{M}_i = \{1, 2, \ldots, 2^nR_{i1}\}$ and sends it to the other terminal. Let $x_i(m_i)$ denotes the codeword of length $n_1$ sent by node $T_i$, $i = 1, 2$. The messages are transmitted through a memoryless Gaussian channel and the relay $R$ receives a signal $y_r$. During the BC phase, the relay generates a codeword $x_r(m_r)$ of dimension $n_2$ from the received sequence $y_r$. The signal $X_r$ is transmitted through a broadcast memoryless channel and the received signal at node $T_1$ is $Y_{1i}$, $i = 1, 2$.

All input distributions are real valued: $X_k \sim \mathcal{N}(0, P_k)$, $k = \{1, 2, r\}$, where $\mathcal{N}(0, P_k)$ denotes a zero mean real Gaussian variable with power $P_k$. The received signals can be modeled as follows:

$$Y_r = h_1X_1 + h_2X_2 + Z_r$$
$$Y_{1i} = h_iX_i + Z_{1i}$$

where $h_i$ denotes the channel coefficient between $T_i$ and $R$, $i = 1, 2$. Without loss of generality, channel reciprocity is assumed, i.e. $h_{1-r} = h_{r-1} = h_i$. $Z_r \sim \mathcal{N}(0, \sigma_r^2)$ is the additive white Gaussian noise at the relay and $Z_{1i} \sim \mathcal{N}(0, \sigma_{1i}^2)$ is the AWGN at node $T_i$, $i = 1, 2$. We assume perfect CSI for all nodes and the noise components are independent of each other and from the channel inputs. In the sequel, we investigate the achievable rates and the design of our scheme.

III. ACHIEVABLE RATE REGION FOR TWRC

Theorem 3.1: Let $(\Lambda_1, \Lambda_2)$, a pair of two nested lattices of dimension $n_1$, with $\Lambda_2 \subset \Lambda_1$. For Gaussian TWRC, the convex hull of the following end-to-end rates $(R_{12}, R_{21})$ is achievable:

$$R_{12} \leq \frac{\alpha}{2} \log_2 \left(1 + \frac{|h_1|^2 \sigma_1^2}{|h_1|^2 \sigma_1^2 + |h_2|^2 \sigma_2^2} \right)$$
$$R_{21} \leq \frac{\alpha}{2} \log_2 \left(1 + \frac{|h_2|^2 \sigma_2^2}{|h_1|^2 \sigma_1^2 + |h_2|^2 \sigma_2^2} \right)$$

where $D_2$ satisfies:

$$\alpha \log_2 \left( \frac{\sigma_2^2}{D_2} \right) + \log_2 (G(\Lambda_1)\mu(\Lambda_2)) \leq (1 - \alpha) \min \left\{ \log_2 \left(1 + \frac{|h_2|^2 \sigma_2^2}{\sigma_2^2} \right), \log_2 \left(1 + \frac{|h_1|^2 \sigma_1^2}{\sigma_1^2} \right) \right\}$$

with $G(\Lambda_1)$ being the normalized second moment of $\Lambda_1$ and $\mu(\Lambda_2)$ being the volume to noise ratio of $\Lambda_2$ [15], and $\alpha \in [0, 1]$.

Remark 1: Letting $n_1 \to \infty$, the left-hand side expression in (5) reduces to its first term since the second term corresponds to the penalty of using finite dimension, that vanishes asymptotically. We have shown in [14] that the achievable rate region coincides with the random coding compress and forward achievable rate region presented in [8].

IV. PROOF OF THEOREM 3.1

In this section, we present a detailed proof of theorem 3.1. The main idea of the proposed scheme is the following: during the BC phase, the relay station sends a compressed version of the signal received during the MAC phase. The relay employs a lossy compression Wyner-Ziv scheme using nested lattices that is tuned to the side information of the user with the weakest side information. The proof is divided into three paragraphs: in section IV-A, we present the WZ strategy based on the weakest side information at the receivers. In section IV-B, the lattice coding scheme for the WZ model is introduced and finally the achievable rates of the proposed scheme are derived in IV-C.

A. Wyner-Ziv using the weakest side information

Let $S_i = h_iX_i$ be the side information available at terminal $T_i$, $i = 1, 2$. Without loss of generality, we assume that $|h_2|^2 P_2 \leq |h_1|^2 P_1$. With this setting, $T_2$ is the terminal who experiences the weakest side information. The quantization performed by the relay is tuned so that $T_2$ reconstructs a local version $\hat{Y}_{r,2}$ of $Y_r$ with a distortion $D_2$: $\frac{1}{n_2} E[\|Y_r - \hat{Y}_{r,2}\|^2] \leq D_2$. The terminal $T_1$ will undergo this choice on its decoded signal at the end of transmission.

The source $Y_r$ can be written as the sum of two independent Gaussian r.v.: the side information $S_2$ and the unknown part $U_2 = Y_r | S_2 = h_1X_1 + Z_r$, that will be decoded at the end. The variance per dimension of $U_2$ is $\sigma_{U_2}^2 = VAR(Y_r | S_2) = |h_1|^2 P_1 + \sigma_1^2$.

B. Lattice based source coding

We use a pair of $n_1$-dimensional nested lattices $(\Lambda_1, \Lambda_2)$ chosen as in [13]: the fine lattice $\Lambda_1$ is good for quantization with basic Voronoi region $V_1$ of volume $V_1$ and second
moment per dimension $\sigma^2(\Lambda_1) = D_2$ and the coarse lattice $\Lambda_2$ is good for channel coding with basic Voronoi region $\mathcal{V}_2$ of volume $V_2$ and second moment $\sigma^2(\Lambda_1) = \sigma_{\tilde{U}_2}^2$.

The encoding operation is performed with four successive operations: first, the input signal $Y_r$ is scaled with a factor $\beta$. Then, a random dither which is uniformly distributed over $\mathcal{V}_1$ is added. This dither is known by all nodes. The dithered scaled version of $Y_r$, $\beta Y_r + t$ is quantized to the nearest point in $\Lambda_1$. The outcome of this operation is processed with a modulo-lattice operation in order to generate a vector $v_r$ of size $n_1$ as shown in Fig.2.

$$v_r = Q_1(\beta Y_r + t) \mod \Lambda_2$$

(6)

The relay sends the index of $v_r$ that identifies the coset of $\Lambda_2$ relative to $\Lambda_1$ that contains $Q_1(\beta Y_r + t)$. The coset leader $v_r$ is represented with $V_2/V_1$. bits. Thus, the source coding rate of the scheme is

$$R(D_2) = \frac{1}{n_1} \log_2 |\Lambda_1 \cap \mathcal{V}_2| = \frac{1}{n_1} \log_2 \frac{V_2}{V_1} \quad \text{(bits per dimension)}$$

(7)

At both users, $v_r$ is reconstructed first. Then $\hat{Y}_{r,i}|\hat{S}_i = \hat{U}_i$ is reconstructed with a WZ lattice decoder (WZLD) using the side information $S_i$ as

$$\hat{U}_i = \beta((v_r - t - \beta S_i) \mod \Lambda_2), \quad i = 1, 2$$

(8)

C. Rate analysis

At the relay, the message $m_r$ corresponding to the index of $v_r$ is mapped to a codeword $x_r$ of size $n_2$. Let $R_r$ be the common broadcast rate. This rate is bounded by

$$n_1 R(D_2) \leq n_2 R_r$$

(9)

On the other hand,

$$R_r \leq \min(I(X_r; Y_1), I(X_r; Y_2))$$

(10)

Since real Gaussian codebooks are used for all transmissions, we have: $I(X_r; Y_i) = \frac{1}{2} \log_2 \left( 1 + \frac{\|x_r\|^2}{\sigma^2(\mathcal{V}_1)} \right), \quad i = 1, 2$. This constraint ensures that the index $m_r$ is transmitted reliably to both terminals and $v_r$ is available at the input of WZLD at both receivers. At terminal $T_2$, $\hat{u}_2$ in (8) can be written as:

$$\hat{u}_2 = \beta((\beta u_2 + e_q) \mod \Lambda_2)$$

(11)

$$\beta(\beta u_2 + e_q) \mod \Lambda_2$$

(12)

where $e_q = Q_1(\beta Y_r + t) - (\beta Y_r + t) = - (\beta Y_r + t) \mod \Lambda_1$, is the quantization error. By the Crypto Lemma [10], $E_q$ is independent from $Y_r$, thus $U_2$, and it is uniformly distributed over $\mathcal{V}_1$ i.e $\text{VAR}(E_q) = \sigma^2(\Lambda_1) = D_2$. The equivalence between (11) and (12) is valid only if $\beta u_2 + e_q \in \mathcal{V}_2$. With finite dimension lattices, the volume of $\mathcal{V}_2$ should be large enough to enclose this signal. In this case, provided that

$$\frac{1}{n_1} \mathbb{E}\|E_q + \beta U_2\|^2 = D_2 + \beta^2 \sigma_{\tilde{U}_2}^2 \leq \sigma^2(\Lambda_2)$$

(13)

The rates are calculated by ensuring that the probability $\text{Pr}(\beta U_2 + E_q \notin \mathcal{V}_2)$ does not exceed a fixed threshold.

$$\text{Pr}(\beta U_2 + E_q \notin \mathcal{V}_2) \leq P_e$$

(14)

Given that $V_1 = \left(\frac{\sigma^2(\Lambda_1)}{G(\Lambda_1)}\right)^{n_1/2}$ where $G(\Lambda_1)$ is the normalized second moment (NSM) of $\Lambda_1$ and $\sigma^2(\Lambda_1) = D_2$, the coding rate in (7) reads:

$$R(D_2) = \frac{1}{2} \log_2 \left( \frac{\sigma_{\tilde{U}_2}^2}{D_2} \right) + \frac{1}{2} \log_2 (G(\Lambda_1) \mu(\Lambda_2))$$

(15)

The WZ rate distortion function is achieved with a redundancy term $L = \frac{1}{2} \log_2 (G(\Lambda_1) \mu(\Lambda_2))$, where

$$\mu(\Lambda_2) = \frac{V_2}{\sigma_{\tilde{U}_2}^2}$$

(16)

is the $\Lambda_2$ volume to noise ratio (VNR) associated with probability of error $P_e$. This term has been introduced by Poltyrev in [16] for lattice codes in AWGN setting. For a probability $P_e$ and a lattice $\Lambda$ with volume $V$, $\mu(\Lambda) = V^{\frac{1}{2}} / \sigma^2$, $\sigma^2$ is the variance of a Gaussian noise $Z$ which verifies $\text{Pr}(Z \notin \mathcal{V}) \leq P_e$. By analogy to our problem, taking into account the constraints expressed in (13) and (14), the VNR is given by (16). Finally, (5) is obtained by combining equations (9), (10) and (15).

The parameter $\beta$ has to be chosen so that to verify (13) and (17).

$$\frac{1}{n_1} \mathbb{E}\|Y_r - \hat{Y}_{r,2}\|^2 = (1 - \beta^2)^2 \sigma_{\tilde{U}_2}^2 + \beta^2 D_2 \leq D_2$$

(17)

Thus, the optimal scaling factor $\beta$ is $\beta = \sqrt{1 - \frac{D_2}{\sigma_{\tilde{U}_2}^2}}$ (see [13]). By replacing $U_2$ by its value we conclude that:

$$\hat{U}_2 = \beta^2 h_1 x_1 + \beta^2 z_2 + \beta e_q$$

(18)

Let $Z_{eq} = \beta^2 z_2 + \beta e_q$ be the effective additive noise. The communication between $T_1$ and $T_2$ is equivalent to a virtual additive Gaussian channel where the noise is given by $Z_{eq}$. Let $Z_{eq}$ a Gaussian variable with same variance as $E_q$. Based on the results in [17], we have

$$\mathcal{D}(\beta^2 U_2 + \beta E_q, \beta^2 U_2 + \beta Z_{eq}) = h(\beta^2 U_2 + \beta Z_{eq}) - h(\beta^2 U_2 + \beta E_q)$$

(19)

where $\mathcal{D}(., .)$ is the relative entropy. Let $\lambda = \frac{D_2}{\sigma_{\tilde{U}_2}^2}$, $M = \frac{E_q}{\sqrt{\lambda}}$ and $M^* = \frac{Z_{eq}}{\sqrt{\lambda}}$, we can verify that

$$h(\beta^2 U_2 + \beta E_q) = h(\sqrt{\lambda} M + \sqrt{1 - \lambda} M^*)$$
Since $U_2$ is Gaussian, this entropy increases to zero monotonically as $D_2$ goes from zero to $\sigma^2_{U_2}$ as shown in [17]. Equivalently for $D_2 \to 0$, the entropy increases to $h(M^*)$:

$$h(\beta^2U_2 + \beta E_q) \to h(M^*) = h(Z_q) - \log_2 2(\sqrt{X})$$

$$= \frac{1}{2} \log_2 (2\pi e D_2) - \frac{1}{2} \log_2 \left( \frac{D_2}{\sigma^2_{U_2}} \right)$$

We have $h(\beta^2U_2 + \beta Z_q) = \frac{1}{2} \log_2 (2\pi e \sigma^2_{U_2})$. Thus from (19),

$$D(U_2, \beta^2U_2 + \beta Z_q) \to -\frac{1}{2} \log_2 \left( \frac{D_2}{\sigma^2_{U_2}} \right) + \frac{1}{2} \log_2 \left( \frac{D_2}{\sigma^2_{U_2}} \right) = 0$$

We conclude that in the divergence sense, for high resolution assumption as $D_2 \to 0$, we can approximate the rate signal with a Gaussian one. Thus the achievable rate of this link satisfies:

$$nR_{12} \leq \frac{n_1}{2} \log_2 \left( 1 + \frac{\beta^2 |h_1|^2 P_1}{\beta^2 \sigma^2 + D_2} \right)$$

by replacing $\frac{n_1}{n_1} = \alpha$ and $\beta$ by its value, (3) is verified. At terminal $T_1$, the decoder is tailored to the side information $S_1$. Thus, at the decoder we subtract $\beta S_1$ and $U_1$ is reconstructed similarly to $U_2$ in (11). Since $\sigma^2_{S_1} \geq \sigma^2_{S_2}$, we have

$$\sigma^2_{U_1} \leq \sigma^2_{U_2},$$

$$\Pr(\beta U_1 + E_q \notin V_2) \leq \Pr(\beta U_2 + E_q \notin V_2),$$

$$D_1 = \frac{1}{n_1} \mathbb{E} \|Y_r - Y_{r,1}\|^2_2 \leq D_2$$

The communication between $T_2$ and $T_1$ is equivalent to a virtual Gaussian channel with an additive noise $Z_{eq}$ and a rate:

$$nR_{21} \leq \frac{n_1}{2} \log_2 \left( 1 + \frac{\beta^2 |h_2|^2 P_2}{\beta^2 \sigma^2 + D_2} \right)$$

which verifies (4) and concludes the proof. The whole coding scheme is summarized in Fig.3.

Remark 2: It is possible to use $S_1$ as the side information for the WZ lattice coding scheme to achieve a controlled distortion $D_1$ at terminal $T_1$. For this purpose, we need two coding layers: a common layer to be sent to both nodes and a refinement layer to be decoded only by the best node $T_1$. In this case, the achievable rates can be ameliorated. This study is under investigation.

V. NUMERICAL IMPLEMENTATION

In this section, we present the achievable rates for practical finite dimensional lattices. In this case, a rate loss is incurred in the coding rate comparing to the WZ rate distortion function as described in previous sections (III and IV). The achievable rate region is calculated by ensuring that the error probability $\Pr(\beta U_2 + E_q \notin V_2) \leq P_e$. The analytical derivation of the error probability for practical lattice pairs is difficult in general since it requires the integration over the Voronoi region of the coarse lattice. Though it can be computed numerically using Monte Carlo integration or approximated by an upper bound.

An approximation of the error probability can be obtained using union bound and Chernoff bound:

$$\Pr(\beta U_2 + E_q \notin V_2) \approx K(\Lambda_2) \exp \left( -\frac{1}{8} \gamma_c(\Lambda_2) \mu(\Lambda_2, P_e) \right)$$

for sufficiently large $\mu(\Lambda_2, P_e)$. $\gamma_c(\Lambda_2) = \frac{d_{min}^2(\Lambda_2)}{V(\Lambda_2)^{2/n_1}}$ is the coding gain of $\Lambda_2$ with $d_{min}(\Lambda_2)$ is the minimum distance between two points in $\Lambda_2$. We choose the VNR in (15) as follows

$$\mu(\Lambda_2, P_e) \approx \frac{8}{\gamma_c(\Lambda_2)} \log_2 \left( \frac{K(\Lambda_2)}{P_e} \right)$$

Note that $\mu(\Lambda_2, P_e) \gg \frac{1}{\gamma_c(\Lambda_2)}$ for small error probability. This guarantees that the union bound approximation is valid and the error probability is upper bounded by $P_e$.

Furthermore, given that the error probability of the scheme is defined by the goodness of the coarse lattice, the performance of the end to end scheme depends more on this lattice rather than the choice of the fine lattice. Therefore, the simple cubic lattice $Z^n$ with NSM $G(\Lambda_1) = \frac{1}{2\pi}$ will be the preferred choice for the fine lattice. In this case, for a good coarse lattice with NSM $G(\Lambda_2) = \frac{1}{2\pi}$, the rate loss with respect to the ideal WZ scheme is only $\frac{1}{12} \log_2 (2\pi e/12)$ = 0.2546 bit per sample. Moreover, in the quantization problem, the choice of the fine (resp. coarse) lattice is equivalent to the choice of the coarse (resp. fine) lattice for the dual channel coding problem. It has been shown in [18] that practically $Z^n$ suffices as a shaping lattice that verifies arbitrary small error probability. Thus, a sublattice of $Z^n$ can be a simple engineering choice for the fine lattice. In the sequel, $\Lambda_1$ is a scaled version of $Z^n_{11}$ i.e. $\Lambda_1 = \eta Z^n$.

We characterize the whole achievable rate region of the proposed scheme by optimizing the time division $\alpha \in [0, 1]$ between MAC and BC phases and the distortion choice at the relay. The boundary bounds are determined by maximizing the weighted sum of both rates $R_{12}$ and $R_{21}$. We solve the following problem for $\theta \in [0, 1]$

$$\max \quad \theta R_{12} + (1 - \theta) R_{21}$$

s.t. $$(R_{12}, R_{21}) \text{ satisfy (3) and (4)}$$

$D_2$ satisfies (5) for $\alpha \in [0, 1]$ (22c)

Table I gives the kissing number and the coding gain for a set of commonly used finite lattices, that can be used to calculate $\mu(\Lambda_2, P_e)$ for fixed $P_e$ using (21). Comparison between lattice pairs can be found in Fig. 4 for symmetric static channels.
In this paper, we derived a new achievable rate region for TWRC with finite dimension. We proposed for this purpose a new practical lattice-based physical layer network coding scheme. The scheme is based on Wyner-Ziv source coding strategy and nested lattice codes. We presented a numerical implementation of the achievable rates with practical finite dimension lattices.

VI. CONCLUSION

In this paper, we derived a new achievable rate region for TWRC with finite dimension. We proposed for this purpose a new practical lattice-based physical layer network coding scheme.

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